

## Particle properties of Waves

### Part 7

#### Problems on Compton Effect & Pair Production

1. X-rays of wavelength 10.0 pm are scattered from a target.

- Find the wavelength of the X-rays scattered through  $45^\circ$ .
- Find the maximum wavelength present in the scattered X-rays.
- Find the maximum kinetic energy of the recoil electrons.

**Solution :**

Given  $\lambda = 10.0 \text{ pm}$

$$\begin{aligned} \text{a) } \lambda' &= \lambda + \lambda_c(1 - \cos\theta) \\ \lambda' &= 10 + 2.426(1 - \cos 45^\circ) \\ &= (10 + 0.7) \text{ pm} = 10.7 \text{ pm} \end{aligned}$$

$$\begin{aligned} \text{b) } \lambda' &= \lambda + 2\lambda_c \\ &= 10 + (2 \times 2.426) \\ &= 14.9 \text{ pm} \approx 15 \text{ pm} \end{aligned}$$

$$\begin{aligned} \text{c) } K &= h\nu - h\nu' \\ K_{max} &= \frac{hc}{\lambda} - \frac{hc}{\lambda'} = hc \left( \frac{1}{\lambda} - \frac{1}{\lambda'} \right) \\ &= 1.6 \times 10^{-6} \text{ eV} \left( \frac{\lambda' - \lambda}{\lambda\lambda'} \right) \\ &= 1.6 \times 10^{-6} \text{ eV} \left( \frac{5 \text{ pm}}{10 \text{ pm} \times 15 \text{ pm}} \right) \\ &= 0.413 \times 10^5 \text{ eV} = 41.3 \text{ KeV} \end{aligned}$$

2. A beam of  $\gamma$  – radiation having photon of energy 510 KeV is incident on a foil of aluminium. Calculate the wavelength of scattered radiation at  $90^\circ$  and direction of the recoil electron.

**Solution :**

Given  $E_i = 510 \text{ KeV}$

$$\theta = 90^\circ$$

$$\lambda' = ?$$

## ENTRI

$$\lambda' - \lambda = \lambda_c(1 - \cos\theta)$$

$$\text{Since } E = hv = \frac{hc}{\lambda}$$

$$\begin{aligned} \lambda &= \frac{hc}{E} = \frac{1.26 \times 10^{-6} \text{ eV}}{510 \times 10^3 \text{ eV}} \\ &= 0.243 \times 10^{-11} \text{ m} \\ &= 2.43 \times 10^{-12} \text{ m} \\ &= 2.43 \text{ pm} \end{aligned}$$

When  $\theta = 90^\circ$

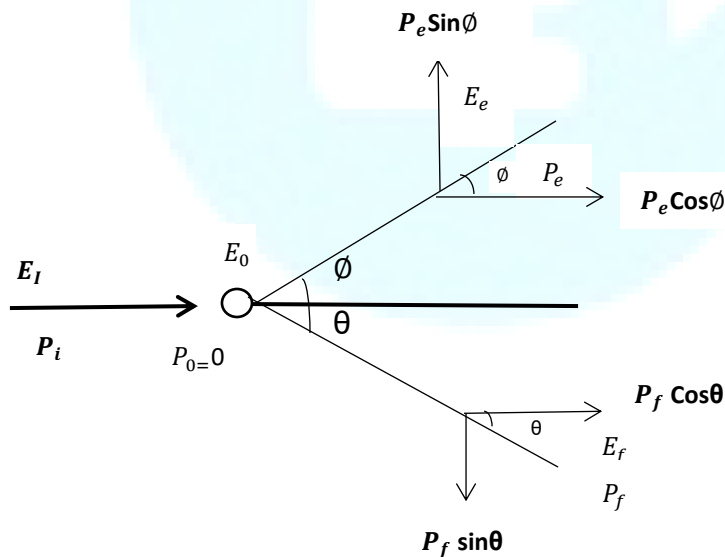
$$\lambda' - \lambda = \lambda_c(1 - \cos 90^\circ) \longrightarrow \lambda' = \lambda + \lambda_c$$

$$\lambda' = 2.43 + 2.42 = 4.8 \text{ pm}$$

$$K = hc \left( \frac{\lambda' - \lambda}{\lambda \lambda'} \right)$$

$$= 1.26 \times 10^{-6} \left( \frac{2.426 \text{ pm}}{2.43 \times 4.8 \text{ pm}} \right)$$

$$K = 25 \times 10^4 \text{ eV} = 250 \text{ KeV}$$



Along X-axis  $P_i = P_e \cos\phi + P_f \cos\theta$

Along Y-axis  $0 = P_e \sin\phi - P_f \sin\theta$

$$P_e \cos\phi = P_i - P_f \cos\theta \longrightarrow (1)$$

$$P_e \sin\phi = P_f \sin\theta \longrightarrow (2)$$

## ENTRI

$$\frac{(2)}{(1)} \implies \tan \phi = \frac{P_f \sin \theta}{P_i - P_f \cos \theta}$$

$$\text{Put } \theta = 90^\circ \quad \tan \phi = \frac{P_f}{P_i} = \frac{P_f}{P_i} \times \frac{C}{C} = \frac{E_f}{E_i}$$

$E = PC$
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$$\frac{E_f}{E_i} = \frac{250 \text{ KeV}}{510 \text{ KeV}}$$

$$\tan \phi = 0.5$$

$$\phi = \tan^{-1} 0.5$$

