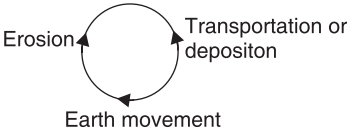


Origin of Soil

1

Soil is an unconsolidated material, composed of soil particles, produced by disintegration of rocks.

Father of Soil Mechanics **Dr. Karl Terzaghi** coined the term “Soil Mechanics” in 1925.



The Geological Cycle

Erosion phase

- | | |
|--|---|
| <p>Physical weathering</p> <ul style="list-style-type: none"> • Retains same composition of Parent rock • Bulky particles • Shape → Angular, Rounded, Flat and Elongated • Single grain without bonding between them | <p>Chemical weathering</p> <ul style="list-style-type: none"> • Change in mineral composition • Plate like with high surface area • Crystalline particle of colloidal size known as clay mineral |
|--|---|

Transportation phase

Soil	Deposited by
Alluvial Soil	River
Marine Soil	Sea water
Locustrine Soil	Still water like lakes
Aeolian Soil	Wind
Glacial Soil	Ice

Note: Loess is an aelian soil.

Various types of Soil

Alluvial soil: Low density and liable to liquefaction in earthquake prone areas.

Black cotton soil: Residual deposits from basalt or trap rocks, contain clay mineral **Montmorillonite**.

Laterite soil: Iron oxide gives red or pink colour. Residual soil formed from basalt.

Desert soil: Uniform in gradation (eg. dune sand). It's Non-plastic and highly pervious.

Marine soil: Low shearing strength. Highly compressible, soft and Highly plastic.

Bentonite: Formed from volcanic ash, with high percentage of Montmorillonite.

Hard pans: Dense, well graded, cohesive aggregates of mineral particle. They do not disintegrate when submerged in water.

Loam: Mixture of sand, silt and clay.

Peat: Organic soil with fibrous aggregate's formed from vegetable matter in excess moisture (eg. in swamps), Highly compressible not suitable for foundation.

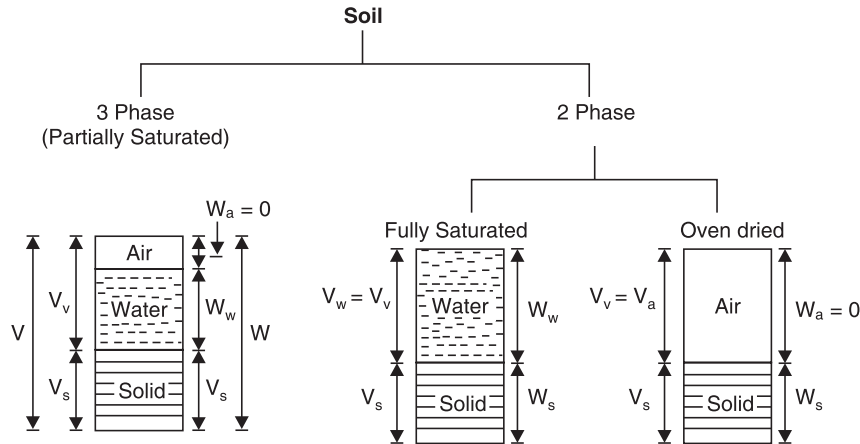
Indurated clay: Hardening of clay due to heat and pressure.

Note: Lithification is a process by which unconsolidated materials are converted into coherent solid rock as by compaction or cementation.

Properties of Soil (Soil-Water Relationship)

Phase diagram

Diagrammatic representation of the different phases in a soil mass.



Water Content

$$w = \frac{W_w}{W_s} \times 100$$

$$0 \leq w < \text{Infinity}$$

W_w = Gravity water + capillary water + Hygroscopic water

W_w can be removed by oven drying.

Void ratio

$$e = \frac{V_v}{V_s} \quad 0 < e < \text{Infinity}$$

Fine grained soil have higher Void ratio than coarse grained soil. While the size of void in coarse grained soil is greater than coarse grained soil.

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Porosity

$$\eta = \frac{V_v}{V} \times 100 \quad 0 < \eta < 100$$

Void ratio serves as a useful parameter as compared to porosity void ratio is defined wrt volume of soil solid's which do not change even in compression.

Degree of Saturation

$$S = \frac{V_w}{V_v} \quad 0 \leq S \leq 100$$

for fully saturated soil $S = 100\%$

for fully dry soil $S = 0\%$

for partially saturated soil $0 < s < 100$

Air content

$$a_c = \frac{V_a}{V_v}$$

Percentage air Void

$$n_a = \frac{V_a}{V} \times 100$$

Percentage air void is always less than air content.

Bulk unit weight

$$\gamma_t = \frac{W}{V} = \frac{W_s + W_w}{V_s + V_w + V_a} \quad \text{units} \rightarrow \frac{\text{KN}}{\text{m}^3}, \frac{\text{N}}{\text{m}^3}, \frac{\text{kgt}}{\text{cm}^3}$$

Unit weight soil

$$\gamma_s = \frac{W_s}{V_s} \quad \gamma_s = G \gamma_w$$

where G = specific gravity of soil solid

Unit weight of water

$$\gamma_w = \frac{W_w}{V_w}$$

Value of γ_w changes with temperature but usually we take

$$\gamma_w = 9.81 \text{ KN/m}^3 \text{ at } 4^\circ\text{C}$$

Dry unit weight

$$\gamma_d = \frac{W_s}{V}$$

High value of γ_d indicates more compacted soil.

Saturated unit weight

$$\gamma_{\text{sat}} = \frac{\text{Wt. of Saturated Soil}}{\text{Volume of Soil}}$$

It's the unit weight of soil when all the air voids are filled with water

Submerged or Bouyant unit weight

$$\gamma_{\text{sub}} = \frac{(W_s)_{\text{sub}}}{V}$$

When the soil is below the water table then a Bouyant force acts on the soil solid and its saturated weight is decreased by unit weight of water.

$$\gamma_{\text{sub}} = \gamma_{\text{sat}} - \gamma_w$$

Note: Saturated soil may or may not be submerged but a submerged soil will always be saturated.

Specific gravity of solids

$$G = \frac{\gamma_s}{\gamma_w} \quad \text{No unit}$$

Also known as "Absolute specific gravity" or 'grain specific gravity'.

Mass specific gravity of solid

$$G_m = \frac{\gamma_t}{\gamma_w} \quad \text{No unit} \quad G_m < G$$

Relative density

$$D_r = \frac{e_{\text{max}} - e_{\text{natural}}}{e_{\text{max}} - e_{\text{min}}}$$

$$= \frac{\gamma_{d \text{ max}}}{\gamma_{d \text{ natural}}} \left(\frac{\gamma_{d \text{ natural}} - \gamma_{d \text{ min}}}{\gamma_{d \text{ max}} - \gamma_{d \text{ min}}} \right)$$

This parameter (D_r) is generally used for sandy and gravelly soils

Relative density	Classification
0 – 15	Very loose
15 – 35	Loose
35 – 65	Medium dense
65 – 85	Dense
85 – 100	Very dense

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Note: For uniformly graded coarse soil having perfectly spherical grain size when particles are arranged in

(a) Cubical array

$$e_{\max} = 91\%; \quad \eta_{\max} = 47.6\%$$

(b) Prismoidal array

$$e_{\min} = 35\%; \quad \eta_{\min} = 25.9\%$$

Some Important Relationships

$$1. W_s = \frac{W}{1+w}$$

$$2. V_s = \frac{V}{1+e}$$

$$3. \gamma_d = \frac{\gamma_t}{1+w}$$

$$4. e = \frac{\eta}{1-\eta}$$

$$5. \eta = \frac{e}{1+e}$$

$$6. Se = wG$$

$$7. \gamma_t = \frac{G+Se}{1+e}$$

$$8. \gamma_{\text{sat}} = \frac{G+e}{1+e} \gamma_w$$

$$9. \gamma_d = \frac{G}{1+e} \gamma_w$$

$$10. \gamma_{\text{submerged}} = \frac{G-1}{1+e} \gamma_w$$

$$11. \gamma_d = \frac{(1-\eta_a)G_s \gamma_w}{1+wG_s}$$

$$12. S = \frac{w}{\frac{\gamma_w}{\gamma_t}(1+w) - \frac{1}{G_s}}$$

Methods of determination of water content

- Over drying method:** Soil sample is derived in controlled temperature (105 – 110°C) for 24 hrs in laboratory. Above 110°C, **water of crystallisation** will be lost

$$w = \frac{w_2 - w_3}{w_3 - w_1}$$

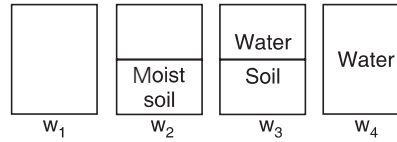
$$w_1 = \text{wt. of container}$$

$$w_2 = \text{wt. of container} + \text{wt. of moist soil}$$

$$w_3 = \text{wt. of container} + \text{of dry soil.}$$

- Torsion balance moisture meter method:** For rapid and accurate determination of water content. Since drying and weighing occur simultaneously, the method is useful for soils which quickly reabsorb moisture after drying.

3. Pycnometer method:



$$w = \left[\left(\frac{w_2 - w_1}{w_3 - w_4} \right) \left(\frac{G - 1}{G} \right) - 1 \right]$$

- This method is more suitable for cohesionless soil as the removal of entrapped air from cohesive soil is difficult. Hence w_3 cannot be measured accurately.

4. Sand bath method:

- Rapid field method, Hence, not accurate.
- Sand bath is a large, open vessel containing sand filled to a depth of 3 cm or more.
- Same formula of oven drying method.

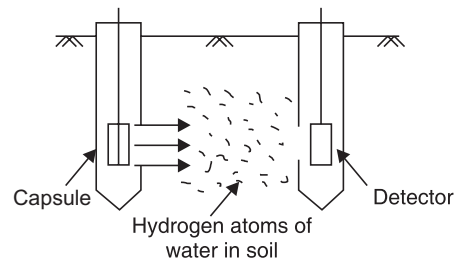
5. Calcium Carbide method

- Quick method but not so accurate.
- $\text{CaC}_2 + 2\text{H}_2\text{O} \rightarrow \text{C}_2\text{H}_2 \uparrow + \text{Ca(OH)}_2$
- Scale is calibrated to give the water content based on total weight (w) of the soil. So, actual water content (based on soil solid) is to be recalculated.

$$\text{Reading given} = w_t = \frac{w_w}{W} = \frac{w_w}{W_s + W_w}$$

$$\text{So } W_w = \frac{w_t}{1 - w_t}$$

6. Radiation method:



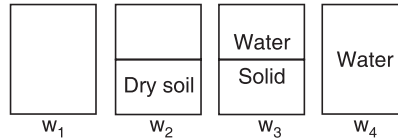
11.10 CIVIL ENGINEERING

- > Gives water content in in-situ condition
- > Loss of energy by radio-active material (cobalt 60) due to scattering of neutrons by hydrogen atoms of soil while travelling from capsule to detector is proportional to water content.

7. Alcohol method:

- > Quick method
- > Not to be used with soils containing calcium compound or organic content.

Determination of specific gravity of soil solid (G)



- Pycnometer method
- SP. gravity values are reported at 27°C
- G can also be determined indirectly by using shrinkage limit.

$$G_T = \frac{W_2 - W_1}{(W_4 - W_1) - (W_3 - W_2)}$$

To remember, Rewrite as

$$G_T = \frac{W_2 - W_1}{(W_4 - W_3) - (W_1 - W_2)}$$

$$\Rightarrow G = \frac{(W_1 - W_2)}{(W_1 - W_2) - (W_4 - W_3)}$$

$$G_{27^\circ\text{C}} = \frac{G_T \times \text{unit wt. of water at } T^\circ\text{C}}{\text{unit wt. of water at } 27^\circ\text{C}}$$

Note: Pycnometer method is used for determination of water content as well as specific gravity. In water content determination, w_2 is the moist soil while in determination of specific gravity w_2 is dry soil.

Determination of Unit Weight

1. Core cutter method

- > Field method suitable for, fine grained and clayey soil.
- > Not suitable for stoney, gravelly soil and dry soil.

$$\gamma_t = \frac{W_2 - W_1}{V}$$

W_2 = wt. of core + soil

W_1 = wt. of core

V = volume of core

$$\gamma_d = \frac{\gamma_t}{1 + w}$$

w = water content

2. Water displacement method

- Suitable for cohesive soils only

$$V = V_w - \left(\frac{W_2 - W_1}{\gamma_p} \right)$$

W_1 = wt. of soil sample

W_2 = wt. of soil sample coated with parathin *wax*.

V_w = volume of water displaced by w_2

γ_p = unit wt. of paraffin *wax*

3. Sand replacement method

- field method
- used for gravelly, sandy and dry soil

4. Water ballon method

- volume of the pit is measured by covering the pit with plastic sheet and then filling it with water.
- wt. of water thus calculated is equal to volume of soil excavated.

5. Radiation method

- Bulk density of in situ soil.
- Quick and convenient.

Index Properties of Soil

Properties which help to access the **engineering behaviour** of soil and which assist in determining its **classification** accurately are termed as index property:



Grain Shape

- Sand and gravel have bulky grains of angular or rounded shape.
- Higher the angularity higher will be shearing strength.

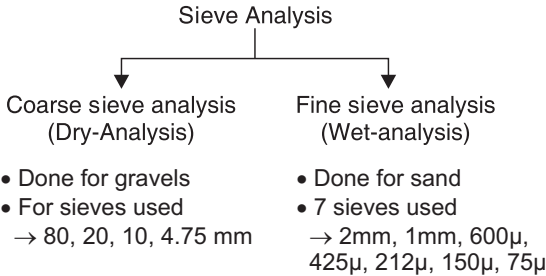
- Sphercity $S = \frac{D_e}{L}$

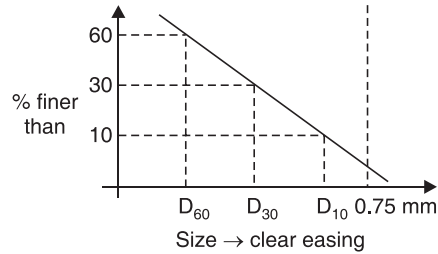
D_e = dia. of equivalent spherical particles

L = Length of particles

where $D_e = \left(\frac{6V}{\pi}\right)^{1/3}$

Gain Size

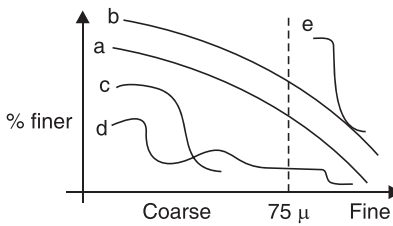


Grain Size Distribution Curves.


D_{10} = effective size of particles i.e. particles which if present alone will cause the same effect as caused by the soil.

D_{60} = Size of the particle such that 60% particle are finer than this size

$$D_{60} > D_{30} > D_{10}$$



a → well graded

a and b → similarly graded

c → poorly/uniformly graded coarse

d → Gap graded

e → Poorly graded fine soil.

Note: If there is a kink in the graph, then it shows the mixture of soil of two different geological formations.

Coefficient of uniformity $C_u = \frac{D_{60}}{D_{10}}$

Coefficient of curvature $C_c = \frac{D_{30}^2}{D_{60} \times D_{10}}$

Sedimentation Analysis,

Stoke's Law: $V_t = \frac{(\gamma_s - \gamma_l)d^2}{18\mu}$

V_t = terminal velocity

d → diameter of the grain

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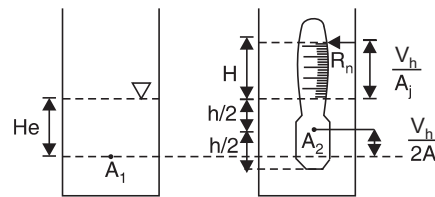
- Range of diameter of particle for stoke's law validity = **0.2 mm to 0.0002 mm**
- If particle size is greater than 0.2 mm, then **turbulent motion** will occur and if particle size is smaller than 0.0002 mm then **Brownian** motion will occur.

$$\frac{h}{t} \propto d^2 \Rightarrow \frac{d_1}{d_2} = \sqrt{\frac{h_1}{t_1} \times \frac{t_2}{h_2}}$$

h = height through which particle falls in t -secs.

Hydrometer Analysis

$$H_e = H + \frac{1}{2} \left(h - \frac{V_h}{A_j} \right)$$



V_h = Volume of hydrometer

A_j = Area of jar

h = length of bulb in hydrometer

Here, H corresponds to reading R_H

Specific gravity of soil suspension at depth H_e

$$G = 1 + \frac{R_h}{1000}$$

$$\frac{(\gamma_s - \gamma_w)d^2}{18\mu} = \frac{H_e}{t} = \frac{H + \frac{1}{2} \left(h - \frac{V_h}{A_j} \right)}{t}$$

Correction's in hydrometer Analysis

Meniscus correction → Always positive (C_m)

Deflocculating Agent correction → Always negative (C_d)

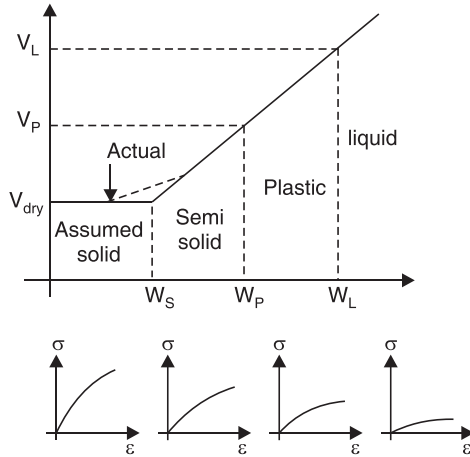
Temperature correction → If temp. is more than its positive otherwise negative (C_t)

Composite correction

$$C = C_m - C_d - C_t$$

Consistency limits

It's the relative ease with which a soil can be deformed. Atterberg classified the consistency in 4-stages → solid, semi-solid, plastic, liquid.



V_L = Volume at liquid limit

V_P = Volume at Plastic limit

V_{dry} = Volume at shrinkage limit

W_L = Water content at liquid limit

W_P = Water content at plastic limit

W_S = Water content at shouunkage limit.

$$\frac{V_L - V_P}{W_L - W_P} = \frac{V_P - V_{dry}}{W_P - W_S}$$

Note: Naturally occurring water content is generally between W_L and W_P

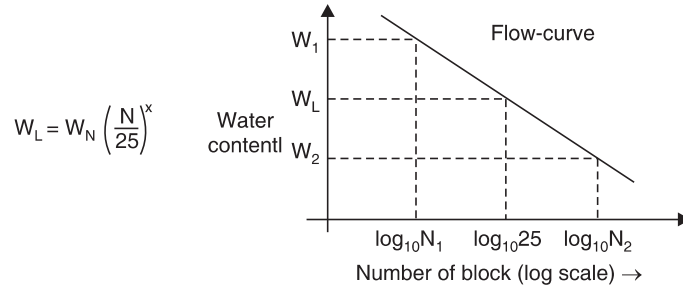
● Volume of soil does not decrease when water content is reduced beyond shrinkage limit.

Liquid limit

Minimum water content at which soil has tendency to flow.

All soils at liouid limit have similar shear strength.

Found out by two tools → (a) Casagrande's (b) Cone penetration. Water content at which 25 blows close the 2mm grove cut in soil sample placed in Casagrande's bowl is called liquid limit

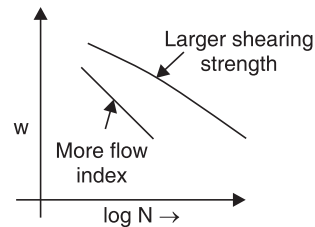


Flow Index (I_p): Slope of flow curve is called flow index

$$I_f = \frac{W_1 - W_2}{\log_{10} N_2 - \log_{10} N_1}$$

$$I_f = \frac{W_1 - W_2}{\log \frac{N_2}{N_1}}$$

$$\text{Flow Index} \propto \frac{1}{\text{Shear Strength}}$$



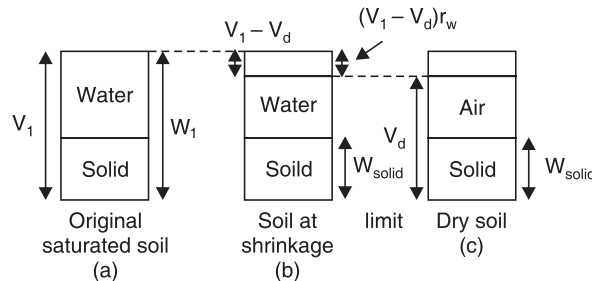
Plastic limit

Minimum water content at which soil is in plastic stage.

At plastic limit, a soil when rolled into a thread of 3 mm starts to crumble shear strength at the plastic limit is about 100 times at the liquid limit.

Shrinking limit

Minimum water content at which soil is completely saturated or the maximum water content at which further reduction in water content does not cause any reduction in the volume of soil sample.



$$\text{Water content at shrinkage limit} = \frac{(W_1 - W_{\text{solid}}) - (V_1 - V_d)\gamma_w}{W_{\text{solid}}}$$

(From figure (b))

$$G = \frac{W_{\text{solid}}}{V_1\gamma_w - (W_1 - W_{\text{solid}})}$$

Shrinkage ratio: Volume change in soil above shrinkage limit expressed as a percentage of dry soil per unit change in water content above shrinkage limit.

$$\text{S.R.} = \frac{\left(\frac{V_1 - V_2}{V_d}\right) \times 100}{W_1 - W_2} \qquad \text{S.R.} = \frac{r_d}{r_w}$$

Note: Shrinkage ratio is the mass specific gravity of the soil in dry state.

$$\text{Volumetric Shrinkage} = \frac{V_1 - V_d}{V_d} \times 100$$

Plasticity Index:

$$I_p = W_L - W_P$$

I_p	Consistency
0	Non Plastic
< 7	Low Plastic
7-17	Medium Plastic
> 17	Highly Plastic

$$I_s = W_P - W_S$$

Consistency Index

$$I_c = \frac{W_L - W}{W_L - W_P}$$

Liquidity Index

$$I_L = \frac{W - W_P}{W_L - W_P} \quad I_c + I_L = 1$$

Shrinkage Index

Solid	Semi solid	Plastic	liquid
$I_L < 0$	$I_L < 0$	$0 < I_L \leq 1$	$I_L > 1$
$I_c > 1$	$I_c > 1$	$0 < I_c < 1$	$I_c < 0$
W_S	W_P	W_L	

Consistency	I_c	I_L
Very stiff	> 1	< 0
Stiff	1-0.75	0-0.25
Medium Stiff	0.75-0.5	0.25-0.5
Soft	0.5-0.25	0.5-0.75
Very Soft	0.25-0	0.75-1
liquid State	< 0	> 1

→ Brittle failure

→ Range of plastic failure

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Toughness Index

$$I_t = \frac{I_P}{I_f} \qquad I_t = \frac{I_P}{I_f} = \log \frac{S_p}{S_f}$$

S_p = Shear strength at plastic limit

S_e = Shear Strength at liquid limit

Note: For $I_t < 1$, soil is friable i.e., get's crushed at plastic limit.

Thixotropy

It is the increase in strength of soil with **passage of time** due to tendency of clay soil to regain its **chemical equilibrium** with the **reorientation** of water molecules in the **adsorbed layer**.

During Pile driving in clayey soil, frictional resistance by soil increases due to property of thixotropy.

Sensitivity (S_t): Degree of disturbance due to remoulding

$$S_t = \frac{\text{Unconfined Compressive Strength due to undisturbed soil}}{\text{Confined compressive strength due to remoulded soil}}$$

$$S_t = \frac{q_u \text{ (undisturbed)}}{q_u \text{ (remoulded)}}$$

1	Insentive (General and Coarse sand)
2-4	Normal
4-8	Sensitive (Silt and Clay)
8-16	Extra
> 16	Quick

Note: Stiff clay having figures and crack have $S_t \leq 1$.

Activity Number (A_c):

$$A_c = \frac{I_P}{\% \text{ of clay size particles}}$$

i.e. size $< 2\phi$

< 0.75	Inactive
0.75 - 1.25	Normal
> 1.25	Active

Note : More activity means more change in volume.

Classification of Soil

4

Soil classification is done on the basis of index properties like grain size distribution and plasticity. Three important systems of classification are

- The Unified Soil Classification System (USCS):** Developed by casagrande for the use in airfield construction. Coarse grained soils were classified on the basis of grain size distribution while fine grained soils on the basis of plasticity characteristics.
- American Association of Stale Highway and Transportation Official (AASHTO):**

Soil are classified into 8 groups from A_1 to A_7 with A_8 for muck or peat
 Group index: $GI = 0.2 a + 0.005 ac + 0.01 bd$

where $a = \% \text{ passing through } 75 \mu \text{ sieve} - 35 \quad 1 \leq a \leq 40$
 $b = \% \text{ passing through } 75 \mu \text{ sieve} - 15 \quad 1 \leq b \leq 40$
 $c = \text{liquid limit} - 40 \quad 1 \leq c \leq 20$
 $d = \text{plasticity index} - 10 \quad 1 \leq d \leq 20$

Group index **0 indicates good subgrade material** while group index of **20 indicates very poor subgrade material.**

- Indian standard soil classification system:** It's given by A-casagrande

Coarse grained soil
 Classified on the basis of
 Particle size, fineness, C_c , C_u

Fine grained soil
 classified on the basis of
 Compressibility, liquid limit,
 plasticity index.

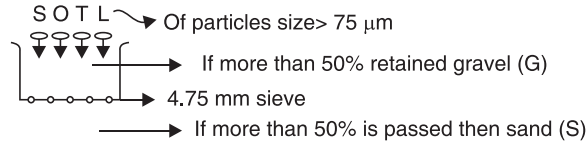
Coarse grained soil classification based on grain size (mm)

Boulder	Cobble	Coarse grained soil					Fine Grained soil	
		Gravel		Sand			silt	clay
		coarse	fine	coarse	medium	fine		
>300	300-80	80-20	20-4.75	4.75-2.0	2-0.425	0.425-0.075	0.075-0.002	<0.002

Note: Fine sand is a coarse grained soil

Coarse grained soil classification

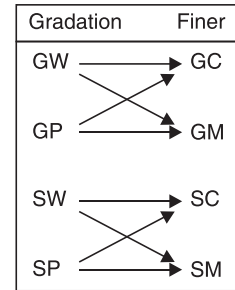
Case 1: When fines i.e. particles less than 75 μm are less than 5%



Well graded gravel (GW)	Poorly graded gravel (GP)
$C_u > 4, 1 < C_c < 3$	Either or both of these are not satisfied
Well graded sand (SW)	Poorly graded sand (SP)
$C_u > 6, 1 < C_c < 3$	Either or both of these are not satisfied

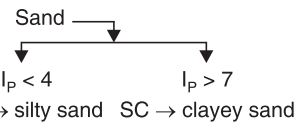
Case 2: When fines are between 5–12 %

- > Dual symbol is used
- > Divided into 8 parts based on gradation and fines
- > For Eq:
 - GW-GM → Well graded gravel with silt as fine
 - SP-SC Poorly graded sand with clay as fines.



Case 3: When fines are greater than 12%

Gravels



Note: If I_p between 4 – 7 dual symbols will be used.

Fine grained soil classification

A –line: $I_p = 0.73 (W_L - 20)$

V – line: $I_p = 0.9 (W_L - 8)$

$W_L < 35,$

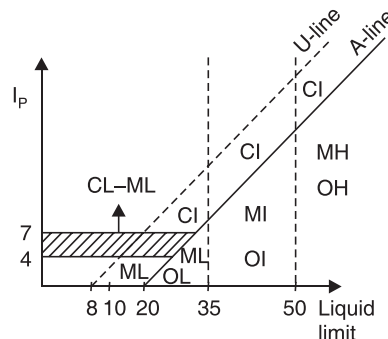
CL → Low plastic **inorganic clay**

ML → Low plastic silt

OL → Low plastic **organic clay**

$35 < W_L < 50,$

CI → Intermediate plastic inorganic clay



MI → Intermediate plastic silt

OI → Intermediate plastic organic clay

$W_L > 50$

CH → Highly plastic inorganic clay

MH → Highly plastic silt

OH → Highly plastic organic clay.

Note: Fine grained soil in indian standard soil classification are sub divided into low, medium, high on the basis of compressibility while in unified soil classification system it has only two categories of low and high compressibility.

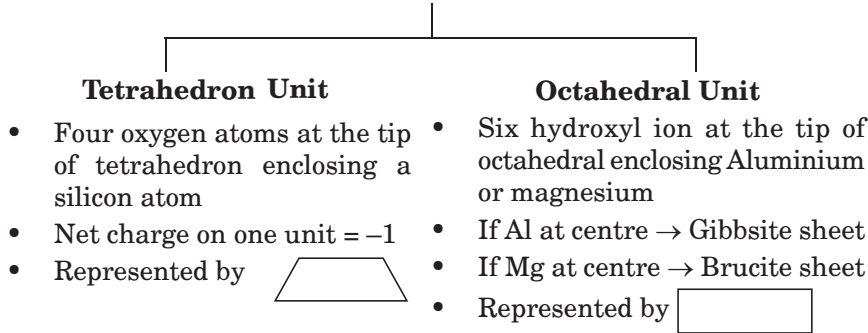
Clay Mineral and Soil-Structure

Properties of coarse grained soil are hardly effected by minerological composition because they are formed due to physical forces and retain the minerological composition of parent rock while properties of fine grain soils like clay depend to a large extent on the nature and characteristics of minerals present.

$$\text{Specific Surface} = \frac{\text{Surface Area}}{\text{Mass or Volume}}$$

Soil Structure

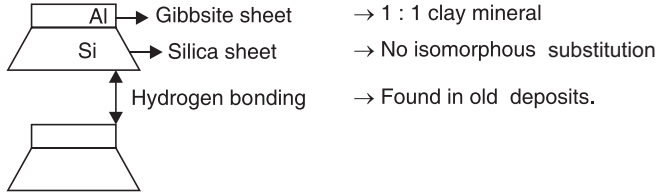
Atomic sturchure of clay mineral



Isomorphic Substitution: Substitution of metallic Ion with another metallic Ion of lower valency but same physical size. for eg Si⁺⁴ replaced by Al⁺³ in a tetrahedral unit.

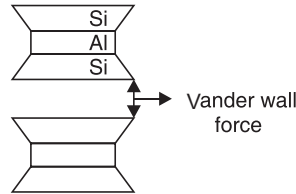
Various Clay Minerals

1. Kaolinite:



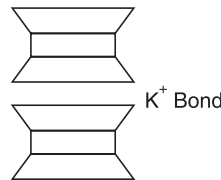
Note: Halloysite when air dried gets converted to Kaolinite and both Halloysite and Kaolinite are used for making chinaware.

2. Montmorillonite:



- 2 : 1 clay mineral
- Highly plastic with little internal friction.
- Common in residual soil derived from volcanic ash.
- Bentonite is a montmorillonite clay.
- Found in Black cotton soil.

3. Illite:



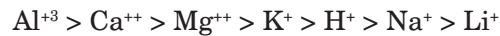
- 2 : 1 clay mineral
- Substantial Isomorphous substitution
- Ionic bonding

Properties of clay minerals

	Grain size	Base exchange capacity	I _p	Dry strength	Activity
Kaolinite	Maximum	Min	Min	Min	Min
Illite	↑	↓	↓	↓	↓
Montmorillonite	Minimum	Max	Max	Max	Max

Cation Exchange capacity: Ability at clay particle to absorb ions on its surface or edge is called base or carbon exchange capacity. It is based on size of particles and mineral structure.

Replacement ability of various cations



Note: Sodium clay is stabilised by using lime by using cation exchange property only.

Compaction of Soil

6

Compaction	Consolidation
Reduction in volume of air voids at a given water content	Volume reduction due to expulsion of pore water from voids
Partially saturated soil	Completely saturated soil
Instantaneous phenomenon	Time dependent phenomenon
Specific compaction Technique	By static load placed on soil

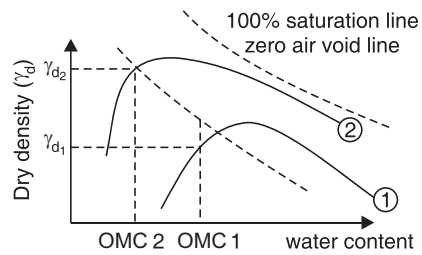
Note: Cohesionless soils are compacted by Vibrations while cohesive soils are compared are compacted by application of static pressure.

Proctor Test

A definite relationship is established between the degree of dry density and soil moisture content. Optimum moisture content (OMC) is the water content at which a particular soil attains maximum dry density (MDD).

- Compactive effort (energy per unit volume) for curve 2 is more than curve 1.

Note: On increasing the compactive effort curve shifts backwards and upwards i.e. OMC decreases and MDD increases.



$$\text{Compactive effort } E = \frac{NnWh}{V}$$

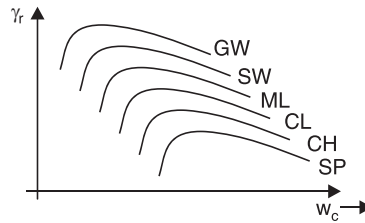
- N → No. of blows per layer
- n → no. of layers
- W → weight of hammer
- h → height of fall
- V → volume of mould

Note: Zero air void line cannot be practically achieved, as all air voids cannot be ever removed.

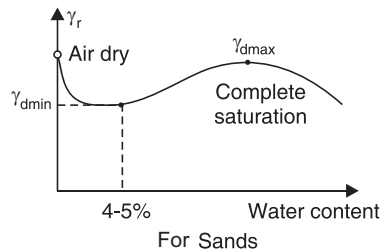
Compaction Tests:

Standard Proctor tests (Light compaction test)	Modified Proctor test (Heavy compaction test)	Indian std. light Compaction test	Indian std. heavy Compaction test
Volume of mould	942 cc	942 cc	1000 cc
No. of layers	3	5	5
No. of blows/layer	25	25	25
Height of free fall	12 inches	18 inches	310 mm
Wt. of hammer	2.495 kg (5.5 lb)	4.54 kg (10 lb)	2.6 kg

Compaction Curve for different Soils:



- Well graded soil can be compacted more than poorly graded soil
- Order of MDD on basis of grain size only
Gravel (G) > Sand (S) > SILT (M) > Clay (C)
- Low plastic soil (L) can achieve higher γ_d than highly plastic (H) soils.



Note: In compaction of sand, initially γ_d decreases due to bulking of sand at nearly 4-5% water content. Then γ_d increases and reaches to maximum at complete saturation.

Suitability of Compaction Equipment

Type of Equipment	Suitable of Soil Type	Nature of project
Rammers or tampers	All soils	In confined areas such as fills behind retaining walls, basement walls, etc. Trench fills.
Smooth wheeled rollers	Crushed rocks, gravels, sands	Road construction, etc.
Pneumatic tired rollers	Sands, gravels silts, clayey soils, not suitable for uniformly graded soils	Base, sub-base and embankment compaction for highways, airfields, etc. Earth dams
Sheepsfoot rollers	Clayey soil, Pure clay	Core of earth dams
Vibratory rollers	Sands	Embankments for oil storage tanks, etc.

Comparison of dry of optimum with wet of optimum compaction

Property	Dry of optimum	Wet of optimum
Structure after compaction	Flocculated (random)	Dispersed (oriented)
Water deficiency	More	Less
Permeability	More, isotropic	Less, anisotropic
Compressibility		
at low stress	Low	Higher
at high stress	High	Lower
Swellability	High	Low
Shrinkage	Low	High
Stress-strain behaviour	Brittle: high peak higher elastic modulus	Ductile: no peak, lower elastic modulus
Construction pore water pressure	Low	High
Strength (undrained) as moulded, after saturation	High somewhat higher if swelling prevented	Much lower Low
Sensitivity	more	Low

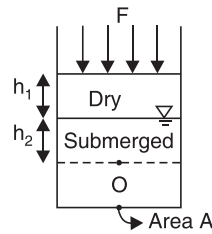
Selection of Compaction water content

Project	Compaction Water Content	Reason
Core of an earth dam	Wet of optimum	To reduce permeability and prevent cracking in core
Homogeneous embankment	Dry of optimum	To have a stronger soil and to prevent build-up of high pore water pressure
Subgrade of pavement	Wet of optimum	To limit volume changes

Effective Stress

7

Effective stress concept is developed by **Terzaghi** and applied to **Fully Saturated** soils only.



$$\bar{\sigma} = \sigma - \mu$$

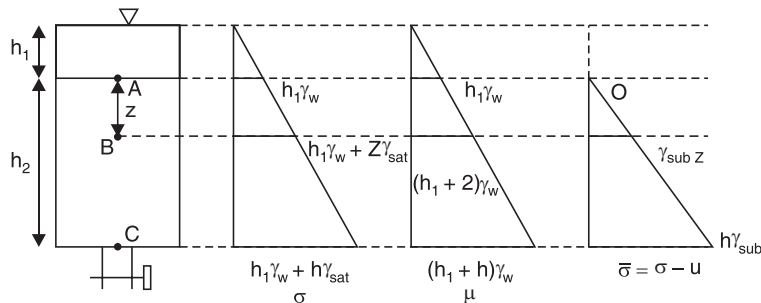
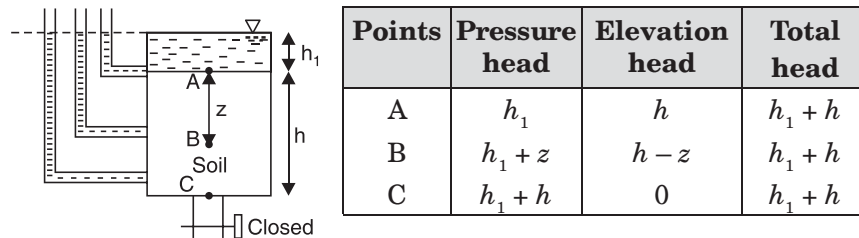
σ = Effective stress
 σ = Total stress
 μ = Pore water pressure

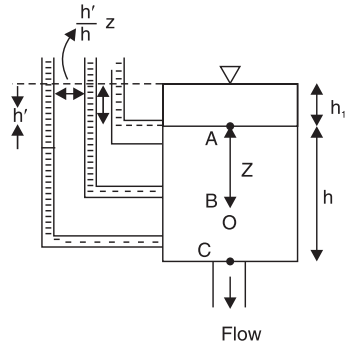
$$\sigma_0 = \frac{F}{A} + \gamma_d h_1 + \gamma_{sat} h_2 \qquad \bar{\sigma}_0 = \frac{F}{A} + \gamma_d h_1 + \gamma_{sat} h_2$$

Note: Effective stress is not a physical parameter hence cannot be measured.

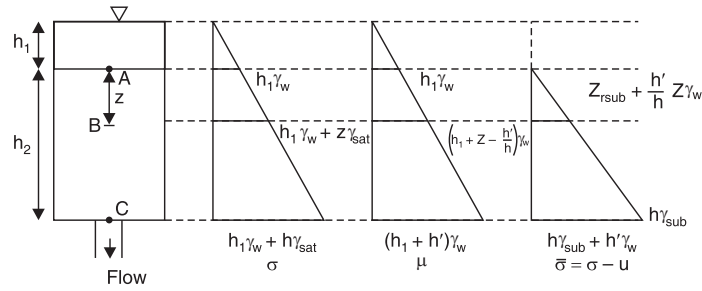
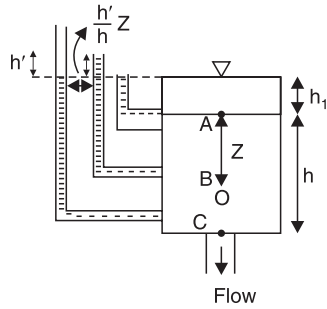
Analysis of Seepage force on effective stress

1. Hydrostatic condition (no flow condition)

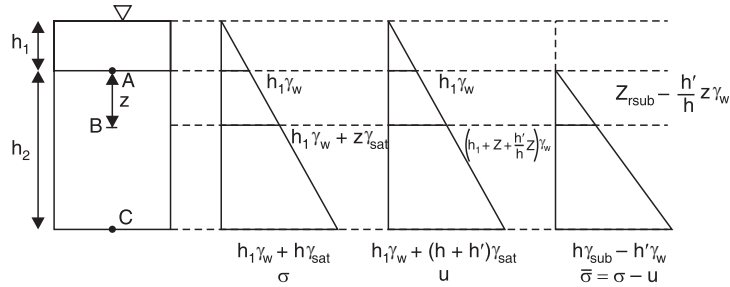


2. Downward flow condition


Po- ints	Pressure head	Eleva- tion head	Total head
A	h_1	h	$h_1 + h$
B	$h_1 + z - \frac{h'}{h}z$	$h - z$	$h_1 + h - \frac{h'}{h}z$
C	$h_1 + h - h'$	0	$h_1 + h - h'$


3. Upward flow condition


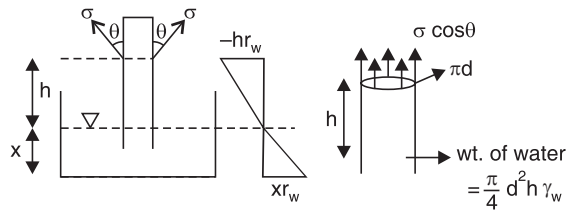
Po- ints	Pressure head	Eleva- tion head	Total head
A	h_1	h	$h_1 + h$
B	$h_1 + z + \frac{h'}{h}z$	$h - z$	$h_1 + h + \frac{h'}{h}z$
C	$h_1 + h + h'$	0	$h_1 + h + h'$



Capillarity and Permeability

8

Water which is held above the water table by phenomenon of surface tension is called capillary water. Due to effect of capillary rise there is increase in unit weight of the soil up to the height of capillary rise



$$\pi d \sigma \cos \theta = \frac{\pi}{4} d^2 h \gamma_w$$

$$h = \frac{4 \sigma \cos \theta}{\gamma_w d}$$

For $\theta = 0^\circ$ $h = \frac{4 \sigma}{\gamma_w d}$

For pure glass,

$$\sigma = 73 \text{ N/m,}$$

$$r_w = 9.8 \text{ kN/m}^3 \quad h = \frac{0.03}{d_{mm}}$$

d = dia of tube in mm

h = height of capillary rise in m

$$h = \frac{0.03}{0.2 D_{10}}$$

D_{10} = Effective size of particle in mm

Other empirical formula:

$$h_{cm} = \frac{C}{e D_{10 \text{ cm}}}$$

c = empirical constant

$$= 0.1 - 0.5 \text{ cm}^2$$

Note: Capillary moisture in fine sand and silt allows unsupported excavation to be made because of stability it provides by virtue of **induced shear** strength.

- Bulking of sand also occurs due to capillarity. It produces **apparent cohesion** which holds the particles in clusters, enclosing honeycombs.

Quick sand condition

In case of **upward seepage flow**, if the upward seepage force becomes equal to the buoyant weight of soil the effective stress in the soil becomes zero.

Critical hydraulic gradient

$$i_{cr} = \frac{\gamma_{sub}}{\gamma_w} = \frac{G - 1}{1 + e}$$

Note: Quick sand condition occurs in sand but not in clay because in clay cohesion exists.

$$\text{Factor of safety} = \frac{i_{cr}}{i_e}$$

i_e = exit hydraulic gradient.

Permeability: It is the ease with which water can flow through any medium.

Darcy's law: In one dimensional flow, discharge through fully saturated soil is given by

$$q = K i A \text{ or } V = Ki \quad i = \frac{\Delta h}{l}$$

q = discharge

A = cross sectional area of the soil corresponding to flow ' q '

i = hydraulic gradient

Δh = loss of head in length ' L '

K = coefficient of permeability

V = Discharge velocity or superficial velocity

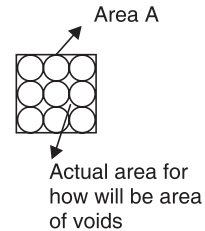
$$(a) V_s = \frac{V}{\eta} \quad V_s > V$$

η = porosity (< 1)

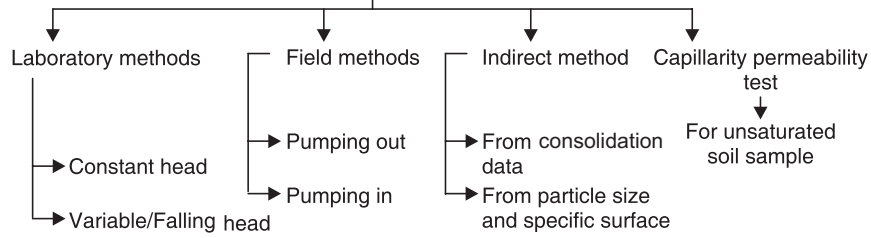
V_s = Actual velocity or seepage velocity corresponding to area of voids in x -sectional area A

$$(b) K_p = \frac{K}{\eta}$$

where K_p = coefficient of percolation.

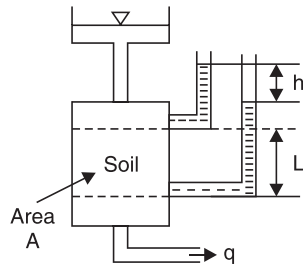


Determination of coefficient of Permeability



Constant head permeability test

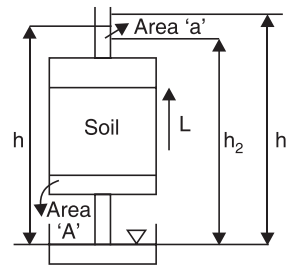
- Coarse grained soil



$$K = \frac{qL}{Ah}$$

Falling head permeability method

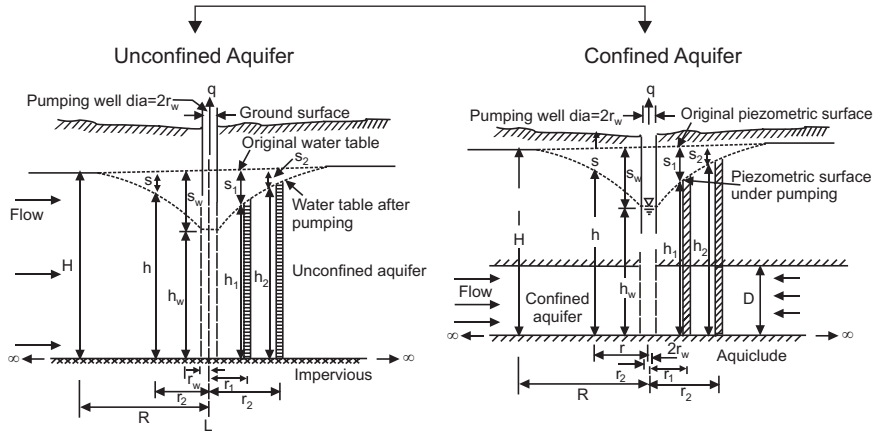
- Fine grained soil.



$$K = \frac{2.303 a L}{A t} \log_{10} \left(\frac{h_1}{h_2} \right)$$

Note: Reliability of laboratory method depends on the extent to which the test specimen represents the original ground conditions.

Pumping out test: Method useful for homogenous coarse grained soil.



$$K = \frac{2.303 q}{\pi (h_2^2 - h_1^2)} \log_{10} \left(\frac{r_2}{r_1} \right) \quad K_2 = \frac{2.303 q}{2\pi D (h_2 - h_1)} \log_{10} \left(\frac{r_2}{r_1} \right)$$

Note: Radius of influence, is the circle over which the effect of pumping is observed. It gradually merges asymptotically to the water table

$$R = 3000 d \sqrt{K} \quad \text{Sichardt's formula}$$

R = radius of influence in m

d = draw down in the well in m

K = coefficient of permeability (m/sec)

Pumping in test: More economical but less reliable than pumping out test as it gives coefficient of permeability of stratum which is close to the hole. It is also of two types.



From consolidation equation:

$$K = c_v m_v \gamma_w$$

c_v = coefficient of consolidation

m_v = coefficient of volume compressibility

γ_w = unit wt. of water.

From particle size and specific surface



$$K = \frac{1}{CS^2} \frac{r_w}{\mu} \frac{e^3}{1+e}$$

C = Shape factor coefficient

S = Surface area per unit volume

$$S = \frac{6}{D} = \frac{6}{\sqrt{ab}}$$

D → dia of particle or size b/w

a_{mm} and b_{mm} .

$$K = CD_{10}^2$$

K → cm/sec

D_{10} → mm

or

$$K = 100 D_{10}^2$$

K → cm/sec

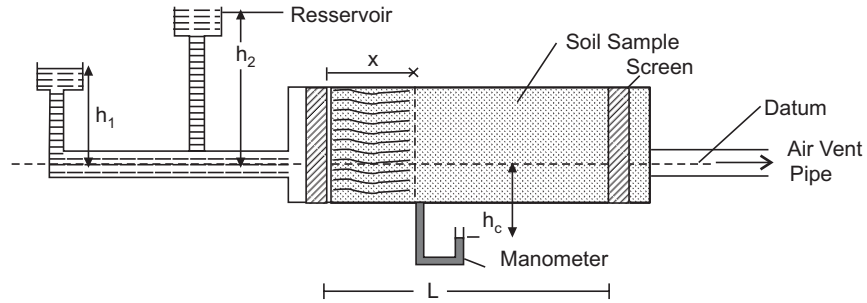
D_{10} → cm

$$\log_{10} (KS^2) = a + b\eta$$

η → porosity

a, b → constants

Capillarity permeability test:



$$\frac{x_2^2 - x_1^2}{t_2 - t_1} = \frac{2K}{S\eta} (h_1 + h_c)$$

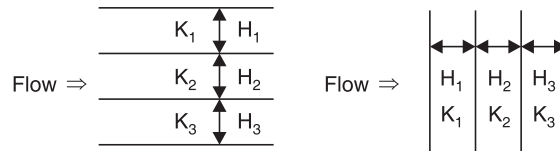
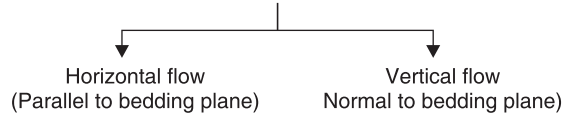
where, S = degree of saturation

η = porosity

h_c = capillary head

water move from x_1 to x_2 in time t_1 to t_2

Permeability of Stratified Soil



$$K_H = \frac{K_1 H_1 + \dots + K_n H_n}{H_1 + H_2 + H_3}$$

$$K_V = \frac{H_1 + H_2 + \dots + H_n}{\frac{H_1}{K_1} + \frac{H_2}{K_2} + \dots + \frac{H_n}{K_n}}$$

Seepage Through Soil

Laplace Equation in two dimensional Flow

$$\frac{\partial^2 \phi}{\partial x^2} + \frac{\partial^2 \phi}{\partial y^2} = 0$$

Potential function $\phi = KH$
 where, H = Total head
 K = Permeability coefficient

$$\frac{\partial^2 H}{\partial x^2} + \frac{\partial^2 H}{\partial y^2} = 0$$

Laplace equation for homogenous **isotropic** soil (in 2D)
 where $\phi = K_x H$ and $\phi = K_y H$ and $K_x = K_y$

$$K_x \frac{\partial^2 H}{\partial x^2} + K_y \frac{\partial^2 H}{\partial y^2} = 0$$

Laplace equation for **Anisotropic** soil (in 2D) where $\phi_x = K_x H$ and $\phi_y = K_y H$ and $K_x \neq K_y$

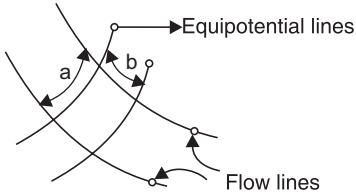
Note: For Anisotropic soil, the section is transformed with x -distance changed to $x \sqrt{\frac{K_y}{K_x}}$ while keeping the vertical dimension constant.

Coefficient of permeability of transformed section $K' = \sqrt{K_x K_y}$ (in 2D).

Calculation of discharge through a flow net

$$q = KH \frac{N_f}{N_d} \left(\frac{a}{b} \right)$$

- q = flow per unit width perpendicular to the pressure plane of section
- H = Total head loss
- N_f = No. of flow channels
- N_d = No. of equipotential drops



11.36 CIVIL ENGINEERING

$$N_f = N_\psi - 1 \quad N_\psi = \text{No. of flow lines}$$

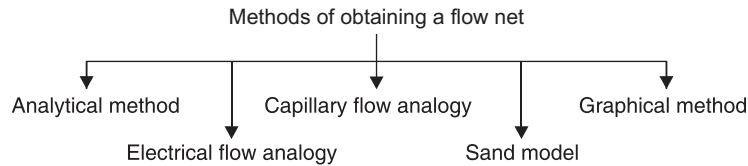
$$N_D = N_\phi - 1 \quad N_\phi = \text{No. of equipotential lines}$$

$$\frac{N_f}{N_D} = \text{Shape factor}$$

$a, b \rightarrow$ dimensions of an elementary square hence ratio of a/b is generally 1

Note: Shape factor (N_f/N_D) is the function of boundary conditions **only**, and will change only when extent of flow is changed. It will not change even if U/S and D/S water levels are interchanged and direction of flow is reversed.

Keeping the boundary conditions same, if the value of N_f is changed then the value of N_D will also be automatically changed in such a way to keep the value of shape factor constant.



Phreatic Line: It is the top flow line which follows the path of base parabola. It is a stream line. The pressure on this line is atmospheric and below this line is hydrostatic.

(a) **Phreatic line with filter**

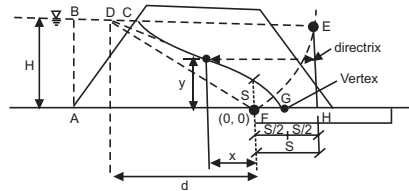
$$x + S = \sqrt{x^2 + y^2}$$

At $x = 0, y = S$

$$\frac{dy}{dx} = \frac{S}{\sqrt{S^2 + 2xS}}$$

At $x = 0, \frac{dy}{dx} = 1$

At F $\frac{dy}{dx} = 1$ and $y = S$ then $q = KS$



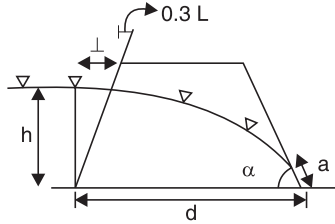
Hence, here q is found out without knowing the complete flownet.

(b) **Phreatic line with out filter**

(i) For $\alpha < 30^\circ$

$$q = Ka \sin^2 \alpha$$

$$a = \frac{d}{\cos \alpha} - \sqrt{\frac{d^2}{\cos^2 \alpha} - \frac{h^2}{\sin^2 \alpha}}$$



(ii) For $\alpha > 30^\circ$

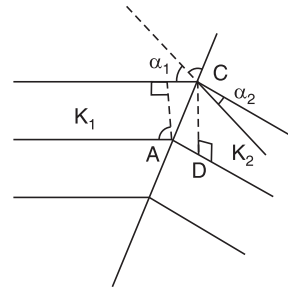
$$q = Ka \sin \alpha \tan \alpha$$

$$a = \sqrt{d^2 + h^2} - \sqrt{d^2 - h^2 \cot^2 \alpha}$$

Flow through Non-homogenous section

$$\frac{K_1}{K_2} = \frac{\tan \alpha_1}{\tan \alpha_2}$$

If $K_1 > K_2$ then $\alpha_1 > \alpha_2$, the flow gets deflected towards the normal otherwise vice a versa.



Filter specifications by Terzaghi

1. **Upper limit** of grain size to ensure **no significant invasion** of particles

$$\frac{D_{15}(\text{filter})}{D_{85}(\text{protected material})} < 5$$

2. **Lower limit** to ensure **sufficient head loss** without excessive seepage pressure

$$4 < \frac{D_{15}(\text{filter})}{D_{15}(\text{protected})} < 20$$

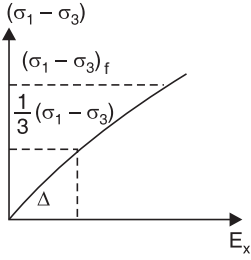
3. Additional guideline

$$\frac{D_{50}(\text{filter})}{D_{50}(\text{protected material})} < 25$$

Vertical Stressess

Modulus of Elasticity of Soil: Determined by **Triaxial** test. It is taken as the **secant** modulus (1/2 to 1/3) of the peak stress. Sometimes initial **tangent modulus** or tangent modulus is also used.

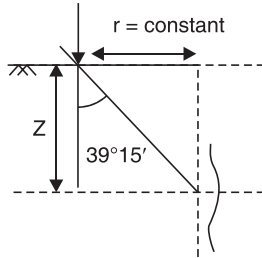
Note: In undrained condition, value of poisson's ratio is 0.5 while in drained condition it's less than 0.5.



Vertical Stress due to concentrated load

<p>Boussineq's (For isotropic soil)</p> $\sigma_{z_b} = \frac{3}{2\pi} \frac{Q}{z^2} \frac{1}{\left(1 + \left(\frac{r}{z}\right)^2\right)^{5/2}}$	<p>Westergaard's Equation (For An-Isotropic soil) Poisson's ratio assumed zero.</p> $\sigma_{z_w} = \frac{1}{\pi} \frac{Q}{z^2} \frac{1}{\left(1 + 2\left(\frac{r}{z}\right)^2\right)^{3/2}}$
---	---

Note: $\frac{r}{z} < 1.5 \quad \sigma_{z_b} > \sigma_{z_w} ; \quad \frac{r}{z} > 1.5 \quad \sigma_{z_b} < \sigma_{z_w}$

Bossinesq's result

 when z is constant

$$\sigma_{z \max} = 0.0888 \frac{Q}{r^2}$$

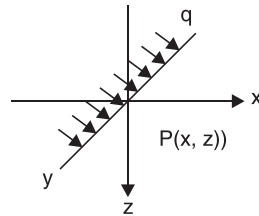
 when r is constant

$$\sigma_{z \max} = 0.1332 \frac{Q}{z^2}$$

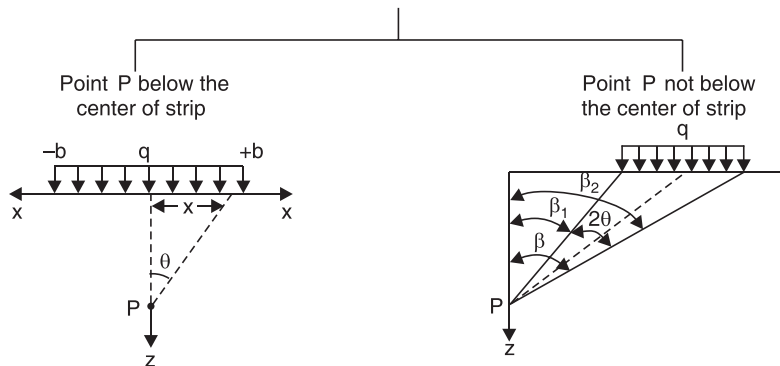
Note: Westergaard's result are more close to the field conditions but Boussinesq results are used for calculation because they provide conservative results.

Vertical stress due to line load

$$\sigma_z = \frac{2q}{\pi z} \left(\frac{1}{1 + \left(\frac{x}{z}\right)^2} \right)^2$$


 \Rightarrow At $x = 0$ at depth z

$$\sigma_z = \frac{2}{\pi} \frac{q}{z}$$

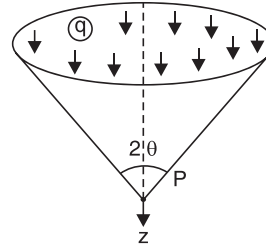
Vertical stress due to strip load


$$\sigma_z = \frac{q}{\pi} (2\theta + \sin 2\theta)$$

$$\sigma_z = \frac{q}{\pi} (2\theta + \sin 2\theta \cos 2\phi)$$

Vertical stress due to a circular area

$$\sigma_z = q (1 - \cos^3 \theta)$$



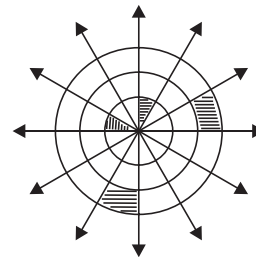
Vertical stress below the corner of a rectangle

$$\sigma_z = \frac{q}{2\pi} \left[\frac{mn}{\sqrt{m^2 + n^2 + 1}} \times \frac{m^2 + n^2 + 2}{m^2 + n^2 + m^2n^2 + 1} + \sin^{-1} \left(\frac{mn}{\sqrt{m^2 + n^2 + m^2n^2 + 1}} \right) \right]$$

where $m = \frac{B}{z}$ $n = \frac{L}{z}$

Note: The value of m and n can be interchanged in equation.

Newmark's Influence chart: Newmark developed the influence chart based on **Boussinesq's** equation to compute **vertical** stress, **horizontal** and **shear** stress due to uniformly loaded area of any shape (regular or irregular) **below** any point, **inside** or **outside** the loaded area



$$\sigma_z = \frac{1}{m \times n} \times q \times N$$

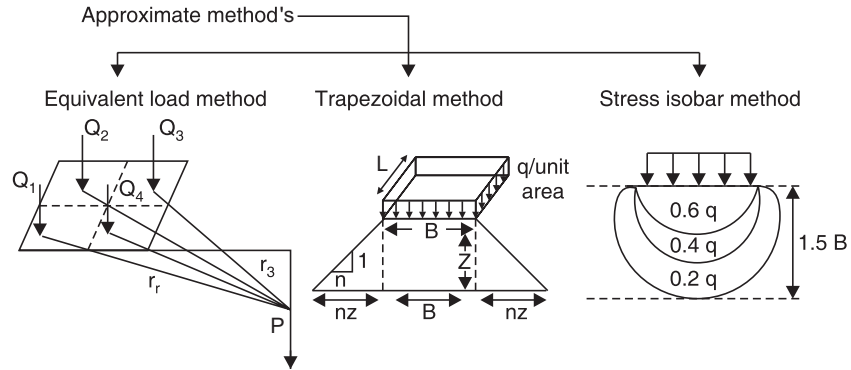
m = No. of concentric circles (normally 10)

n = No. of radial lines (normally 20)

q = Intensity of load

N = Equivalent no. of areas

All the area units will have equal influence at the center whether the area is inside or outside the loaded area, it will have the same influence at the center of the chart.



$$\sigma_z = \sigma_{z_1} + \sigma_{z_2} + \sigma_{z_3} + \dots$$

$$\sigma_{z_1} = K_{B_1} \frac{Q_1}{z^2} \quad \sigma_{z_2} = K_{B_2} \frac{Q_2}{z^2}$$

$$\sigma_z = \frac{q(B \times L)}{(B + 2nz)(L + 2nz)}$$

$0.2 q = 20\%$
 Stress isobar
 Area bounded by $0.2 q$ Stress isobar is considered to be stressed by vertical stress on loading.

Compressibility and Consolidation

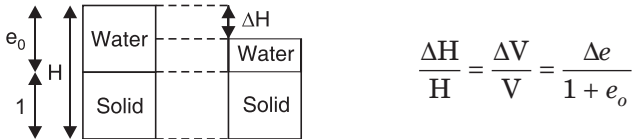
Settlement

Gradual sinking of the structure due to compression of the soil below

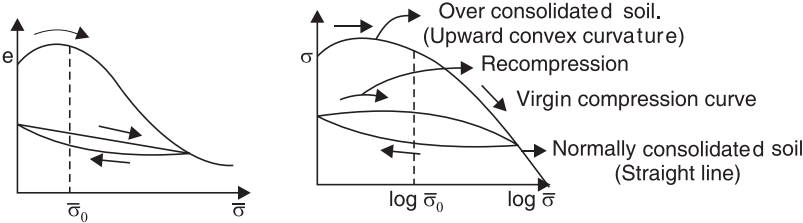
$$S_t = S_{\text{immediate}} + S_{1^{\circ}\text{-consolidation}} + S_{2^{\circ}\text{-consolidation}}$$

Due to **expulsion of air** or compression of pore air
 Due to **expulsion of excess pore water pressure** generated due to increases in **Total stress**.
 Due to gradual re-adjustment of clay particles into more stable configuration under **constant effective stress**.

Note: one dimensional consolidation (ie zero lateral strain) is measured by oedometer test/consolidation test.



Compressibility characteristics



$$\frac{\bar{\sigma}_0}{\sigma} = \text{Over consolidation ratio (OCR)}$$

$\bar{\sigma}_0$ = Pre consolidation stress

If existing effective stress $\bar{\sigma} > \bar{\sigma}_0$, then soil is normally consolidated

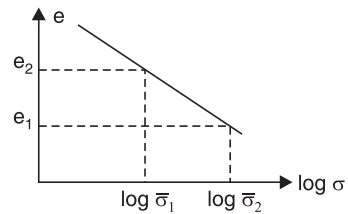
ie OCR = 1

If $\bar{\sigma} < \bar{\sigma}_0$, then over consolidated soil an i.e. OCR > 1

Coefficients in Compressibility of clay

1. Compression index c_c

$$c_c = \frac{e_1 - e_2}{\log_{10} \bar{\sigma}_2 - \log_{10} \bar{\sigma}_1} = \frac{\Delta e}{\log_{10} \left(\frac{\bar{\sigma}_2}{\bar{\sigma}_1} \right)}$$



(a) $c_c = 0.009 (w_L - 10)$ undisturbed soil of medium sensitivity,
 w_L = liquid limit %

(b) $c_c = 0.007 (w_L - 7)$ Remoulded soil of low sensitivity

(c) $c_c = 0.4 (e_o - 0.25)$ undisturbed soil of medium sensitivity

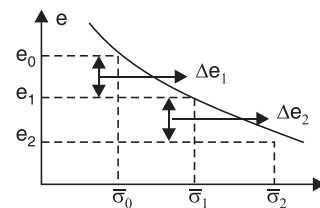
(d) $c_c = 1.15 (e_o - 0.35)$ Remoulded soil of low sensitivity.

Note: c_c has a **constant value** for a given type of soil and is not a function of effective stress.

2. Coefficient of Compressibility (α_v)

$$\alpha_v = \frac{\Delta e}{\Delta \bar{\sigma}}$$

$\Rightarrow \alpha_v$ decreases with the increase in effective stress.



3. Coefficient of volume compressibility (m_v)

$$m_v = \frac{\text{Volume change per unit volume}}{\text{Increase in effective stress}}$$

$$m_v = \frac{\alpha_v}{1 + e_0} \quad e_0 = \text{Initial void ratio}$$

\Rightarrow value of m_v depends on stress range and is not constant for a particular soil.

$$\Rightarrow \text{compression modulus } E_c = \frac{1}{m_v}$$

Computation of Primary Settlement

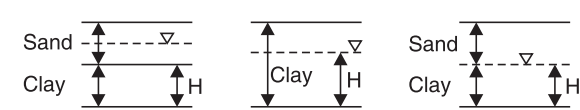
H_0 = Depth in clay below water table only

ΔH = Change in depth (settlement)

e_0 = Initial void ratio.

$$1. \frac{\Delta H}{H} = \frac{\Delta e}{1 + e_0}$$

$$2. \Delta H = m_v \Delta \sigma H_0$$

$$3. \Delta H = \frac{c_c H_0}{1 + e_0} \log \left(\frac{\bar{\sigma}_0 + \Delta \bar{\sigma}}{\bar{\sigma}_0} \right)$$


$$4. \text{Over consolidated soil } \bar{\sigma}_0 + \Delta \sigma < \bar{\sigma}_c$$

$$\Delta H = \frac{c_r H_0}{1 + e_0} \log \left(\frac{\bar{\sigma}_0 + \Delta \bar{\sigma}}{\bar{\sigma}} \right)$$

Normally consolidated soil $\bar{\sigma}_0 + \Delta \bar{\sigma} > \bar{\sigma}_c$

$$\Delta H = \frac{c_r H_0}{1 + e_0} \log \left(\frac{\bar{\sigma}_c}{\bar{\sigma}_0} \right) + \frac{c_c H_0'}{1 + e_0'} \log \left(\frac{\bar{\sigma}_0 + \Delta \bar{\sigma}}{\bar{\sigma}_c} \right)$$

Computation of Secondary Settlement:

$$\Delta H = \frac{c_\alpha H_0}{1 + e_0} \log_{10} \frac{t_2}{t_1}$$

e_0 = void ratio at the end of 1^o settlement

H_0 = height at the end of 1^o settlement.

$$c_\alpha = \frac{\Delta e}{\log(t_2/t_1)} = \frac{\Delta e}{\Delta \log t}$$

c_α is 4-6% of the value of $\frac{c_c}{1 + e_0}$

Terzaghi's one dimensional consolidation equation:

$$\frac{\partial u}{\partial t} = c_v \frac{\partial^2 u}{\partial z^2}$$

u = excess pore pressure

$\frac{\partial u}{\partial t}$ = Rate of change of pore pressure with time

where $C_v = \frac{K}{m_v \gamma_w}$ C_v = coefficient of consolidation

$\frac{\partial u}{\partial z}$ = Rate of change of pore pressure with depth

Time factor (T_v):

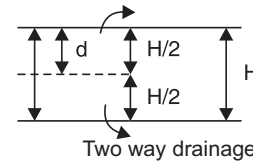
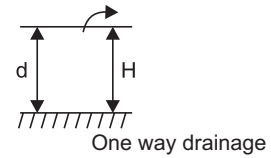
$$T_v = \frac{C_v t}{d^2}$$

C_v = coefficient of consolidation in cm^2/sec

d = length of drainage path

$d = H$ in one way drainage

$d = \frac{H}{2}$ in two way drainage



(a) $u \leq 60\%$ $T_v = \frac{\pi}{4} (u)^2$ u = Avg. degree of consolidation

(b) $u > 60\%$ $T_v = 1.781 - 0.933 \log (100 - u)$

$$T_{50} = 0.196$$

$$T_{90} = 0.848$$

Degree of consolidation

(a) $U = \frac{\Delta h}{\Delta H} \times 100$

Δh = settlement at any stage

ΔH = settlement at end of consolidation.

(b) $U = \frac{e_o - e}{e_o - e_f}$

e_o = initial void ratio

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e = void ratio of any stage

e_f = final void ratio

$$(c) \quad U = \frac{U_i - U}{U_i - U_f}$$

U_i = Initial pore water pressure

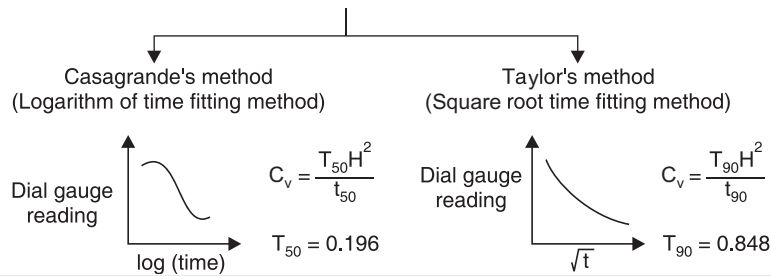
U = Pore water pressure at any stage

$$(d) \quad U = \frac{U_i - U_z}{U_i}$$

U_f = Pore water pressure at the end of stress increment

U_z = excess pore pressure at any depth Z .

Determination of coefficient of consolidation (C_v)



Note: C_v is inversely proportional to liquid limit (w_L) where as c_c is directly proportional to liquid limit.

Value of C_v decreases with increases in plasticity.

Compression Ratio's

$$(a) \text{ Initial compression ratio } r_0 = \frac{R_i - R_0}{R_i - R_f}$$

$$(b) \text{ 1}^\circ \text{ - consolidation ratio } r_p = \frac{R_o - R_{100}}{R_i - R_f}$$

$$(c) \text{ 2}^\circ \text{ - consolidation ratio } r_s = 1 - (r_0 + r_p)$$

$$r_s = \frac{R_{100} - R_f}{R_i - R_f}$$

R_i = initial dial gauge reading

R_0 = Dial gauge reading for beginning of 1° - consolidation

R_{100} = Dial gauge reading for completion of 1° - consolidation

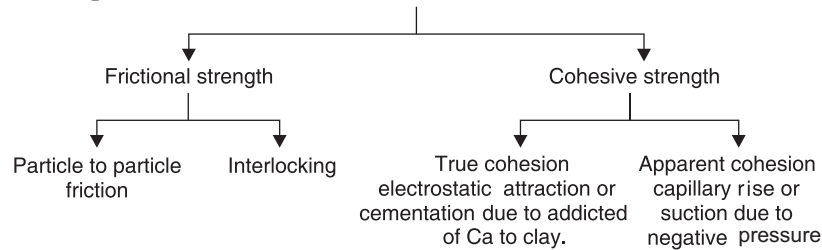
R_f = final dial gauge reading

Shear Strength of Soil

12

It is the capacity of the soil to resist shearing stress. It is defined as the maximum value of shear stress that can be mobilised within a soil mass.

It depends on two factors



Note: Whatever be the nature of loading on soil, failure on soil occurs by shearing, it never occurs by crushing of particles.

Mohr's hypothesis: Shear stress on failure plane at failure reaches a value which is a unique function of normal stress on that plane.

$$\tau_{ff} = f(\sigma_{ff})$$

τ_{ff} = Shear stress on failure plane at failure

σ_{ff} = Normal stress on failure plane at failure.

Coulomb's hypothesis:

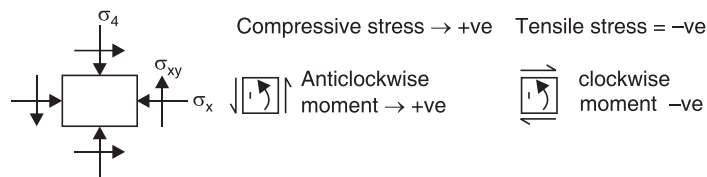
$$\tau_f = C + \sigma \tan \phi$$

$$\tau_f = C' + \bar{\sigma} \tan \phi'$$

where C, ϕ are total stress parameters and C', ϕ' are effective stress parameters.

Note: Shear strength parameter's C, ϕ , C', ϕ' are not the inherent properties of soil. They are related to the type of test and the condition under which these are measured.

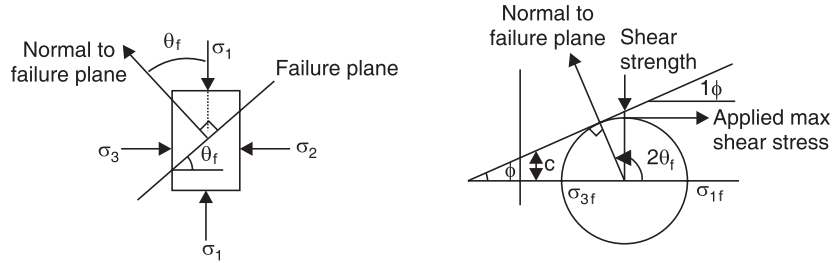
Sign Convention for drawing Mohr's circle



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Relation between of ϕ_p , ϕ , σ_{1f} and ϕ_{3f}

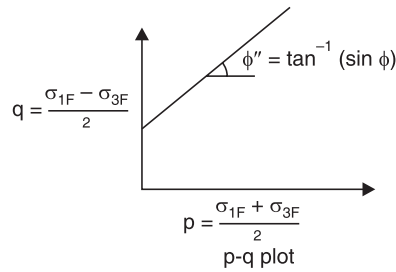
Based on Mohr's Colomb's failure envelope



$$\theta_f = 45 + \frac{\phi}{2}$$

i.e. failure plane makes an angle of $(45 + \phi/2)$ degree with major principal plane

$$\frac{\sigma_{1f} - \sigma_{3f}}{2} = \frac{\sigma_{1f} + \sigma_{3f}}{2} \sin \phi + C \cos \phi$$



$$\sigma_{1f} = \sigma_{3f} \tan^2 \left(45 + \frac{\phi}{2} \right) + 2C \tan \left(45 + \frac{\phi}{2} \right)$$

$$\sigma_{3f} = \sigma_{1f} \tan^2 \left(45 - \frac{\phi}{2} \right) - 2C \tan \left(45 - \frac{\phi}{2} \right)$$

Stability analysis based on drainage conditions

Drained Condition: If the rate of loading is such that water in the pores of soil gets sufficient time to drain out, the condition of loading is called drained condition.

Undrained Condition: The rate of loading is rapid such that the water in the pores does not gets sufficient time to drain out, that condition of loading is called undrained condition.

Note: Both drained and undrained conditions depends on rate of loading and type of soil. Hence these conditions are actually relative.

(a) Shear strength under drained condition

- Effective stress approach is used
- Drained analysis is used to evaluate long term stability.

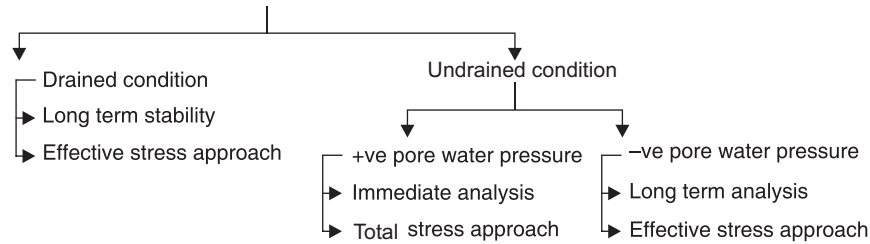
(b) Shear strength under undrained condition

(i) +ve excess pore water pressure develops

- Total stress approach is used
- Shear strength evaluated at the end of construction period

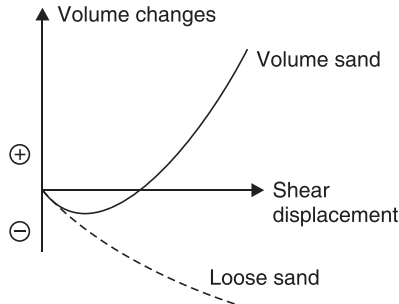
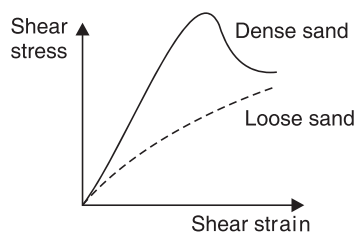
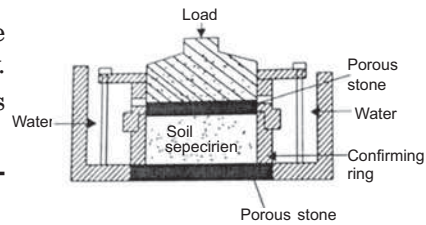
(ii) -ve excess pore water pressure develops

- Effective stress approach is used
- Long term stability is analysed



Direct shear test

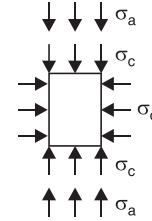
- Good for free draining soil like sand and gravel not used for clay.
- Effective stress and total stress are same
- Shear normally applied at **constant rate of strain**
- Shear and vertical deformations are measured during test using dial gauge



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Triaxial test

- Suitable for all types of soil
- Pore water pressure can be measured under undrained condition.
- Volume change can also be measured under drained condition.



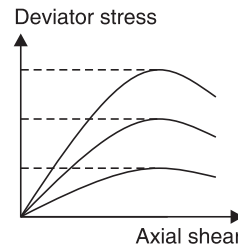
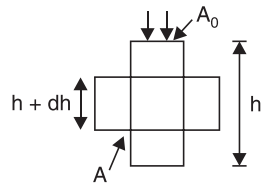
$$\sigma_3 = \sigma_c = \text{confining pressure}$$

$$\sigma_1 = \sigma_c + \sigma_a \quad \sigma_a = \text{deviator stress.}$$

$$\sigma_c = \bar{\sigma}_{V_0} \left(\frac{1 + 2K_0}{3} \right)$$

K_0 = Coefficient of earth pressure at rest = $1 - \sin \phi$
 $\bar{\sigma}_{V_0}$ = Vertical effective stress in the field.

$$\sigma_a = \sigma_1 - \sigma_3 = \frac{\text{Axial load}}{\text{Corrected area}}$$



$$A(h + dh) = V = V_0 + dV$$

$$A = \frac{A_0(1 - \epsilon_v)}{(1 - \epsilon_a)}$$

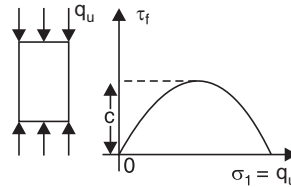
For undrained test $\epsilon_v = 0$

So
$$A = \frac{A_0}{1 - \epsilon_a}, \quad \epsilon_a = \frac{dh}{h}$$

Note: At any time in triaxial test either pore water line is open and drainage line is closed or vice-versa, i.e. either pore water pressure measurement will be made under undrained condition or volume change is measured under drained condition.

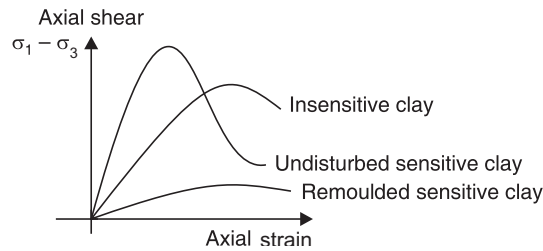
Unconfined Compression Test (UC Test)

- For fully saturated soil. (otherwise $\phi \neq 0$)
- No confining pressure is applied ($\sigma_c = 0$)
- Used to test cohesive soil, in non-cohesive soil sample cannot be prepared without confining pressure.



$q_u =$ unconfined compressive strength

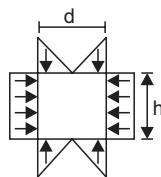
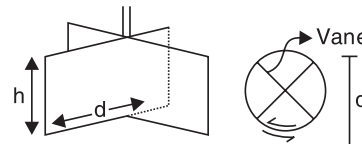
$$q_u = \frac{P}{A_f} = \frac{P}{\left(\frac{A_0}{1 - \epsilon_a}\right)}$$



- Used for rapid assesment of **consistency**.
- Also used for finding **sensitivity** of clay soil, other than fissured clay.

Vane Shear test

- For plastic cohesive soil which is very sensitive
- Maximum torque applied is the total shear



$$\tau_f = \frac{T}{\pi d^2 \left(\frac{h}{2} + \frac{d}{6}\right)}$$

[when both top and bottom end shear the soil]

$$\tau_f = \frac{T}{\pi d^2 \left(\frac{h'}{2} + \frac{d}{12}\right)}$$

[when top end does not shear's the soil n']

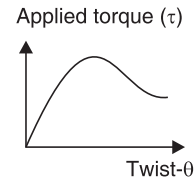
$h' \rightarrow$ height of vane used in shearing.

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Here, $\tau_f = \text{Shear strength} = C_u$ (undrained cohesion)

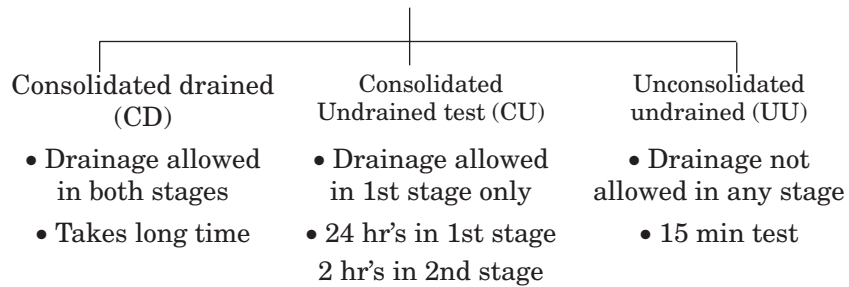
$$C_u = \frac{q_u}{2}$$

$$\text{Sensitivity} = \frac{C_{u \text{ undisturbed}}}{C_{u \text{ remoulded}}}$$



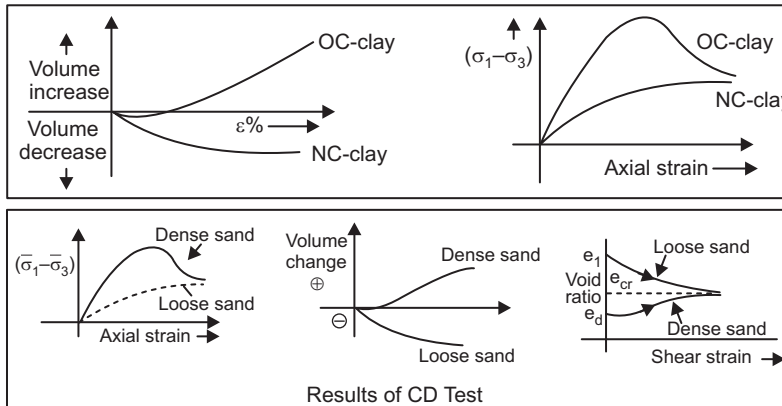
	Lab size	Field size
Height of Vane (H)	20 mm	10–20 cm
Dia of Vane (D)	17 mm	10 cm
Thickness of Vane (t)	0.5–0.1 mm	2–3 cm

Type of Triaxial Tests



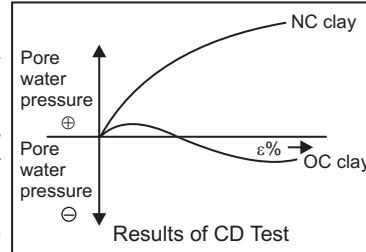
Consolidated Drained Test

- Used in Analysis of gradual loading condition
- To check long term stability of embankment which has been in existence since long



Consolidated Undrained Test

- Sudden unloading such as draw down or dewatering
- Unloading of an embankment that has lived some of its life (i.e. already consolidated)
- Gives both total stress and effective stress parameters



Unconsolidated Undrained test

- Test is suitable for soil of low permeability or when loading is very fast.
- Total stress analysis is performed as it is an undrained test.
- Used in sudden loading such as rapid construction
- Short term stability under pore water pressure.



Note: $\frac{C_u}{\bar{\sigma}_\tau} = 0.11 + 0.0037 I_p \%$

For NC clays, shear strength depends on plasticity Index.

Soil Liquefaction: The phenomenon in which **Saturated loose sand** in **undrained** condition under rapid loading develops **positive pore water pressure** which ultimately reduces the **effective stress to zero**, is called liquefaction. It occurs at high frequency of Vibration e.g. during pile driving, vibration of machine, explosive blasting and earthquake shock.

Pore Pressure Coefficients: It is used to express the response of pore water pressure to change in total stress under undrained conditions and enable the initial value of pore water pressure to be determined.

$$\Delta u = B[\Delta\sigma_3 + \Delta(\Delta\sigma_1 - \Delta\sigma_3)]$$

$$\Delta U_1 = B\Delta\sigma_3$$

$$\Delta U_2 = AB (\Delta\sigma_1 - \Delta\sigma_3)$$

$$B = \frac{\Delta U_1}{\Delta\sigma_3}$$

ΔU_1 = Change in pore pressure due to increase in cell pressure

ΔU_2 = Change in pore pressure due to increase in deviator stress.

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- For saturated soil $B = 1$
- For dry soil $B = 0$
- B varies with the stress range
- A can be found from CD test
- B can be found from first stage in UU test and AB from its second stage.
- A is also not a constant, depends on type of soil, stress condition etc.
- For a given soil A depends on strain, sample distribution, anisotropy and OCR.

Value of A	Type of Soil
- 0.5 to 0	Heavily over consolidated Soil
< 0	Over consolidated soil
0.5-1	Normally consolidated soil
2-3	Loose saturated time sand

Stability of Slopes

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Assumption's in analysis of slope stability

- (a) Slope–stability problem is a two dimensional problem.
- (b) Shear parameters of the soil are constant along any possible slip surface.
- (c) In problems involving seepage of water, flow net can be constructed and the seepage force can be determined.

Stability of Infinite Slope

$$F.O.S = \frac{\tau_f}{\tau}$$

$$F.O.S = \frac{C + \sigma \tan \phi}{\gamma z \cos \beta \sin \beta}$$

(a) $F = \frac{\tan \phi}{\tan \beta}$

when $C = 0$

$$\sigma = \gamma z \cos^2 \beta$$

(b) $F = \frac{C + \gamma z \cos^2 \beta \tan \phi}{\gamma z \cos \beta \sin \beta}$

(c) $F = 1$, and $Z = H_c$ then

$$H_c = \frac{C}{\gamma \cos^2 \beta (\tan \beta - \sin \phi)}$$

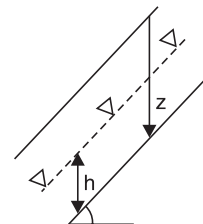
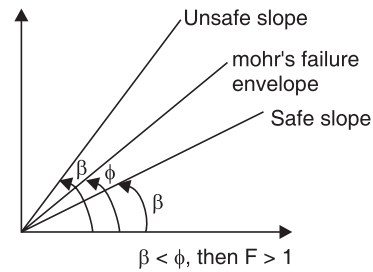
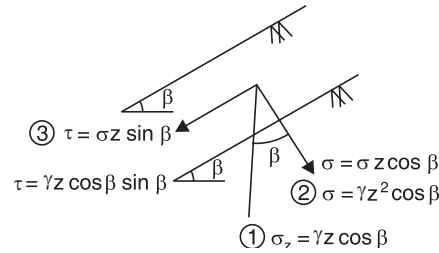
(d) $S_n = \frac{C}{\gamma H_c} = \cos^2 \beta (\tan \beta - \sin \phi)$

Hence, S_n is a dimensionless Quantity

(e) Seepage taking place and W.T. is parallel to the slope in cohesionless soil.

$$F_s = \left[1 - \left(\frac{\gamma_w}{\gamma} \right) \left(\frac{h}{z} \right) \right] \frac{\tan \phi'}{\tan \beta}$$

ϕ' = effective friction angle



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γ = avg. total unit weight of the soil above the slip surface upto the ground level.

$$\gamma = \frac{\gamma_1 h_1 + \gamma_2 h_2}{h_1 + h_2}$$

(f) If water table is at ground level

$$F_s = \frac{\gamma'}{\gamma_{sat}} \frac{\tan \phi}{\tan \beta} \approx F_s = \frac{1}{2} \frac{\tan \phi}{\tan \beta}$$

(g) Infinite slope of purely cohesive soil.

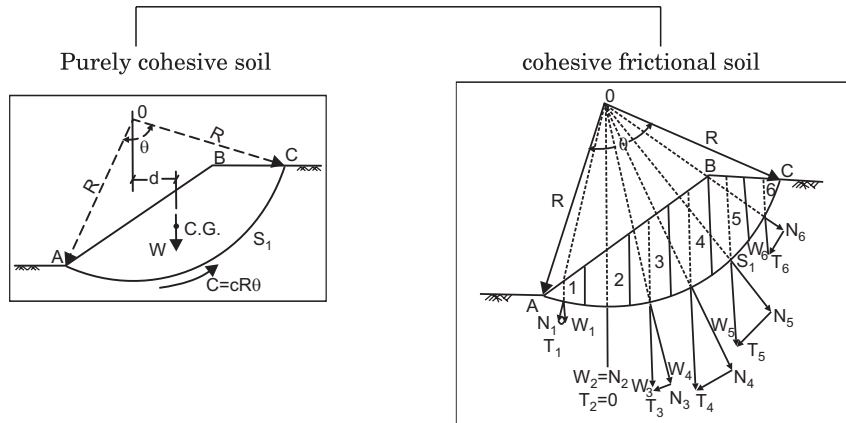
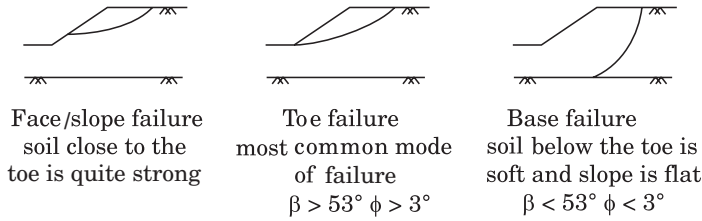
$$F_c = \frac{C}{\gamma z \sin \beta \cos \beta}$$

(h) C - ϕ soil in infinite slope

$$F_s = \frac{C}{\gamma z \sin \beta \cos \beta} + \frac{\tan \phi}{\tan \beta}$$

Stability of Finite Slope

(a) **Swedish Circle Method:** Surface of sliding is assumed as “arc of circle”

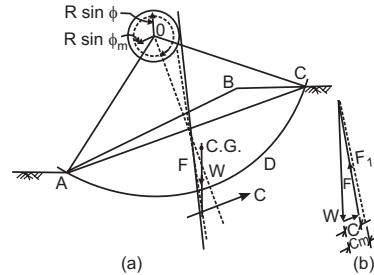


$$F = \frac{CR^2\theta}{Wd}$$

$$F = \frac{CR\theta + \sum N \tan \phi}{\sum T}$$

(b) **Friction Circle Method:** This method is based on the assumption that the resultant force R on the rupture surface is **tangential** to a circle of radius $r = R \sin \phi$ which is concentric with the trial slip circle.

- friction is assumed to be fully mobilised
- Total stress approach is used



$$F_c = \frac{C}{C_m}$$

$$F_\phi = \frac{\tan \phi}{\tan \beta} = \frac{\tan \phi}{\tan \phi_m}$$

(c) **Taylor's stability number:** It's a **dimensionless** parameter. It is obtained for factor of safety wrt cohesion while the factor of safety wrt friction F_ϕ is assumed to be unity.

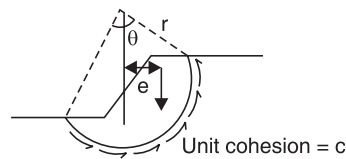
$$S_n = \frac{C}{\gamma H_C} = \frac{C}{\gamma F_C H}$$

In case of saturated slope replace γ by γ_{sat}° while in submerged slope replace it by γ' .

$$\phi_w = \frac{\gamma'}{\gamma_{sat}} \phi$$

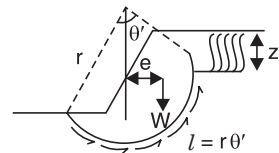
ϕ_w = weight friction angle.

(d) **Fellinius Methods:** For purely cohesive soil



$$F = \frac{Cr^2\theta}{We}$$

r = radius of rupture curve



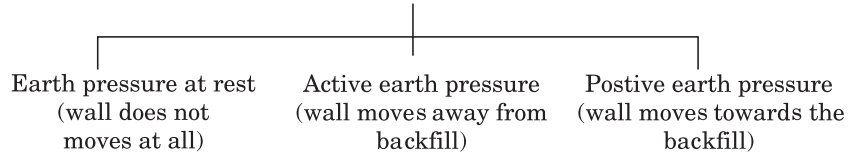
$$F = \frac{Cr^2\theta'}{We}$$

$$Z_c = \frac{2C}{\gamma}$$

Earth pressure and Retaining walls

Earth pressure is the lateral force exerted by the soil on any structure retaining that soil. There are several types of retaining structure's like retaining walls (gravity type, cantilever type, counter fort type), bracings in cuts, abutment of a bridge, sheet pile/anchored sheet pile.

Type's of lateral earth pressure



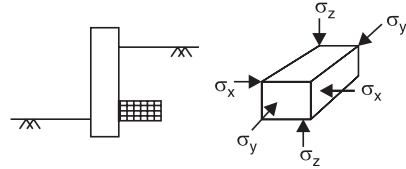
1. Earth pressure at rest

$$\Rightarrow \sigma_x = \sigma_y \text{ and } \epsilon_x = 0$$

$$\text{So } \sigma_x = \frac{\mu}{1 - \mu} \sigma_z$$

$$\sigma_x = K_0 \sigma_z$$

$$\text{Hence, } K_0 = \frac{\mu}{1 - \mu}$$



$$\Rightarrow \text{For cohesion less soil } (C = 0) K_0 = 1 - \sin \phi$$

$$\Rightarrow \text{For normally consolidated soil (N. C. Soil)}$$

$$K_0 = 0.19 + 0.233 \log (I_p)$$

$$\Rightarrow \text{For over consolidated soil (OC soil) } K_{0(oc)} = K_{0(NC)} \sqrt{O.C.R}$$

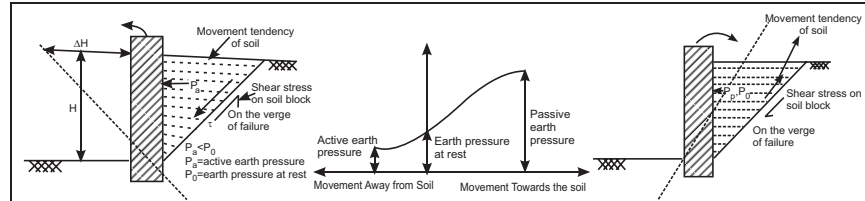
where OCR = over consolidation ratio.

Type of soil	K_0
Dense sand	0.4 – 0.5
Loose sand	0.45 – 0.5
Mechanically compacted	0.8 – 1.0
N.C clays	0.5 – 0.6
O.C clays	1.0 – 4.0

Note: K_0 for dens sand is lesser than that of loose sand.

For NC clays $K_0 < 1$

For OC clays $K_0 > 1$

Active earth pressure and passive earth pressure


Active earth pressure	Passive earth pressure
⇒ Failure plane is inclined at $45 + \phi/2$ with the horizontal	⇒ Failure plane is inclined at $45 - \phi/2$ with the horizontal
⇒ Very little movement is required to mobilise the active pressure	⇒ much higher movement is required to mobilise the pressure
$\Delta H = 0.2\%$ of H Dense sands	$\Delta H = 2\%$ of H Dense sands
$\Delta H = 0.5\%$ of H loose sands	$\Delta H = 15\%$ of H loose sands
$\Delta H = 0.4\%$ of H clay's	
⇒ length of failure block	
$= H \cot \left(45 + \frac{\phi}{2} \right)$ $\Rightarrow K_q = \frac{1 - \sin \phi}{1 + \sin \phi} = \tan^2 \left(45 + \frac{\phi}{2} \right)$	⇒ length of failure block = $H \cot \left(45 - \frac{\phi}{2} \right)$
	$\Rightarrow k_p = \frac{1 + \sin \phi}{1 - \sin \phi} = \tan^2 \left(45 + \frac{\phi}{2} \right)$

Earth pressure theories

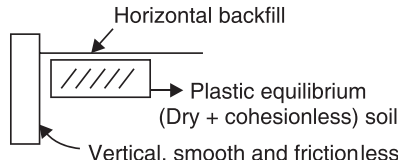
1. Rankine theory (1857)
2. Coulomb's theory (1776)

Note: Coulomb's theory came before Rankine's theory and was even more versatile as it considered friction between wall and the soil but it is still not used because this theory does not satisfies the static equilibrium condition occuring in nature. The three forces do not meet at a common point when sliding surface is assumed to be planer.

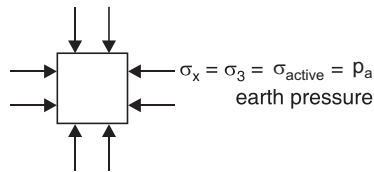
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Rankine's theory **over estimates the active earth pressure** and **under estimates the passive earth pressure** and as retaining walls are designed for active earth pressure hence, Rankine theory gives more conservative results.

- Rankine's theory.** Originally Rankine's theory was only for cohesionless soil but later it was extended to cohesive as well as submerged soil.



(a) Active earth pressure



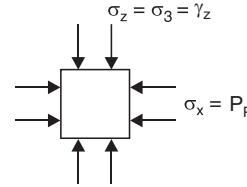
$$p_a = k_a \gamma z - 2c\sqrt{k_a}$$

$$\text{where } k_a = \frac{1 - \sin \phi}{1 + \sin \phi} = \tan^2 \left(45 - \frac{\phi}{2} \right)$$

(b) Passive earth pressure

$$P_p = k_p \gamma z + 2c \sqrt{k_p}$$

$$\text{where } k_p = \frac{1 + \sin \phi}{1 - \sin \phi} = \tan^2 \left(45 + \frac{\phi}{2} \right)$$

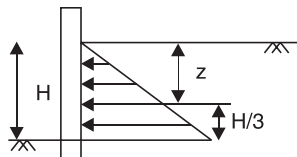


Note: By compacting soil active earth pressure decreases where as passive earth pressure increases

$$k_a = \frac{1}{k_p}$$

Various cases of earth pressures

- Cohesionless soil on a vertical smooth wall**



$$p_{az} = k_a \gamma z$$

$$p_{ap} = k_p \gamma z$$

$$F_a = \frac{k_a \gamma H^2}{2} \quad F_p = \frac{k_p \gamma H^2}{2}$$

(6) Soil with Inclined back fill

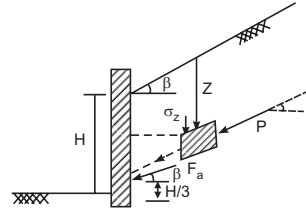
$$\sigma_z = \gamma z \cos \beta$$

$$p_a = k_a \gamma z \cos \beta$$

$$K_a = \frac{\cos \beta - \sqrt{\cos^2 \beta - \cos^2 \phi}}{\cos \beta + \sqrt{\cos^2 \beta - \cos^2 \phi}}$$

$$K_p = \frac{\cos \beta + \sqrt{\cos^2 \beta - \cos^2 \phi}}{\cos \beta - \sqrt{\cos^2 \beta - \cos^2 \phi}}$$

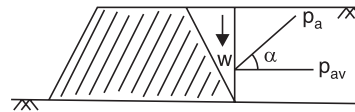
$$F_a = \frac{k_a \gamma H^2}{2} \cos \beta$$


7. Horizontal back fill with inclined wall

$$P_a = \sqrt{W^2 + p_{av}^2}$$

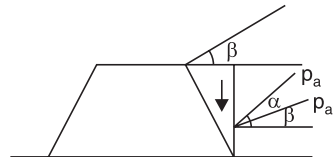
$$p_{av} = \frac{1}{2} k_a \gamma H^2$$

$$\tan \alpha = \frac{W}{p_{av}}$$


8. Inclined back fill with inclined wall

$$P_a = \sqrt{P_{av}^2 + W^2 + 2P_{av} W \sin \beta}$$

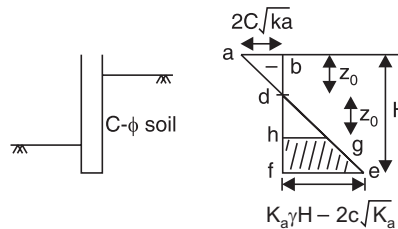
$$\tan \alpha = \frac{W + P_{av} \sin \beta}{P_{av} \cos \beta}$$


9. Active earth pressure on cohesive soil.

$$H_C = 2 z_0 = \frac{4C}{\gamma \sqrt{K_a}}$$

No-contact loss = Active earth pressure corresponds to area efg

After contact loss = Active earth pressure corresponds to area fde



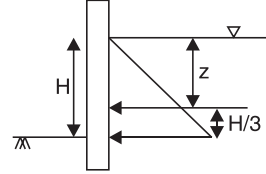
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2. Submerged cohesionless soil on vertical smooth wall

$$p_{az} = k_a \gamma_{sub} Z + \gamma_w Z$$

$$p_{pz} = K_p \gamma_{sub} Z + \gamma_w Z$$

$$F_a = \frac{K_a \gamma_{sub} H^2}{2} + \frac{\gamma_w H^2}{2}$$



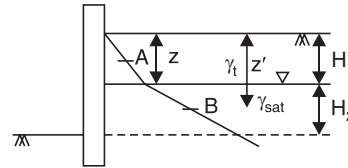
3. Partially submerged cohesionless soil on vertical smooth wall

For point A

$$p_a = k_a \gamma_t z$$

For point B

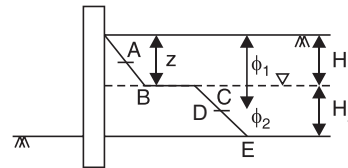
$$p_a = K_a \underbrace{(\gamma_t H_1 - \gamma_{sub} (Z' - H_1))}_{\text{Effective stress}} + \gamma_w (Z' - H_1)$$



Note: water pressure due hydrostatic condition is same in all directions hence hydrostatic pressure is not multiplied by k_a

4. Back fill with two different soils (ϕ_1 and ϕ_2)

A: $p_a = K_{a1} \gamma_2 Z$
 B: $p_a = K_{a1} \gamma_1 H_1$
 C: $p_a = K_{a2} \gamma_1 H_1$
 D: $p_a = K_{a2} (\gamma_1 H_1 + \gamma_2 (Z' - H_1))$
 E: $p_a = K_{a2} (\gamma_1 H_1 + \gamma_2 H_2)$



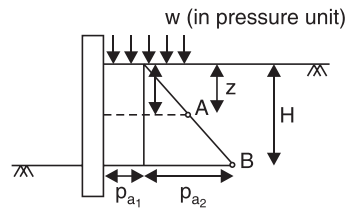
5. Soil with surcharge load

$$p_a = p_{a1} + p_{a2}$$

A: $p_{a1} = k_a w$

$$p_{a2} = k_a \gamma z$$

B: $p_{a1} = k_a w$ $p_{a2} = k_a \gamma H$



$$F = K_{a1} w H + \frac{k_a \gamma H^2}{2}$$

For No contact loss

$$F_a = \left[\frac{K_a \gamma Z^2}{2} - 2C \sqrt{K_a} Z + \frac{2C^2}{\gamma} \right] - \left[\frac{1}{2} \times \frac{2C}{\gamma \sqrt{K_a}} \times 2C \sqrt{K_a} \right]$$

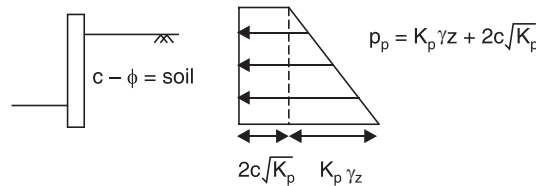
$$F_a = \frac{K_a \gamma Z^2}{2} - 2C \sqrt{K_a} Z$$

After contact loss

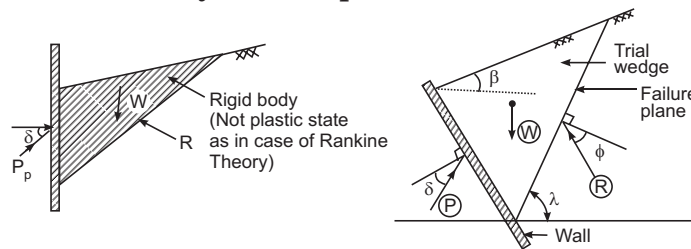
$$F_a = \frac{K_a \gamma Z^2}{2} - 2C \sqrt{K_a} Z + \frac{2C^2}{\gamma}$$

Note: As there is no net earth pressure upto a depth of $2Z_0$ we can make unbraced cut in clayey soil upto depth of $2Z_0$, i.e. $\frac{4C}{\gamma \sqrt{K_a}}$

10. Passive earth pressure on cohesive soil:



Coulomb's theory of earth pressure:



Here sliding wedge is assumed as a at an angle λ from horizontal rigid body.

Forces acting on trial wedge will be W, R, P whose directions will be known. The position and line also of action of earth pressure will also be known in advance. By assuming various trial wedges at different trial angle λ the value of P will be calculated.

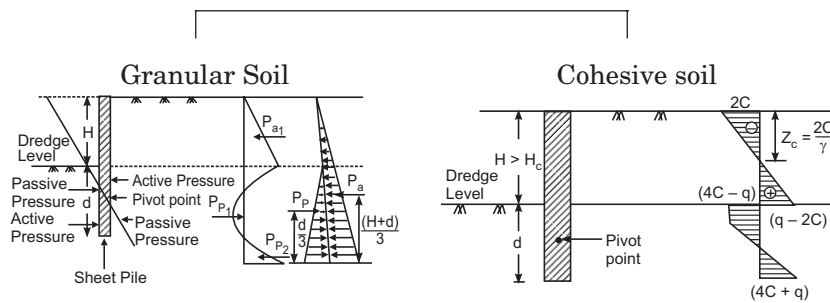
Highest value of P is for active earth pressure while lowers value of P is for passive earth pressure.

Cantilever Sheet Pile and Anchored Bulkhead

15

A sheet pile wall is an earth and water retaining structure which behaves as a fixed vertical cantilevers in resisting lateral earth pressure

Cantilever sheet pile



$$P_p \cdot \frac{d}{3} = P_a \frac{(H + d)}{3} \text{ without FOS}$$

$$\frac{P_p}{\text{FOS}} \times \frac{d}{3} = P_a \frac{(H + d)}{3} \text{ with FOS}$$

$$P_p = \frac{1}{2} K_a \gamma d^2$$

$$P_p = \frac{1}{2} K_a \gamma (H + d)^2$$

$$q = \gamma H$$

At depth H,

$$P_a = q - 2C$$

$$P_p = 2C$$

Resultant at depth H,

$$P_p - P_a$$

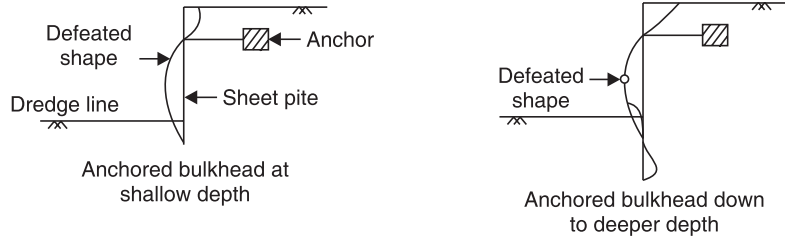
$$P_p - P_a = 4C - q$$

Resultant earth pressure at H + d

$$P_p - P_a = 4C \pm q$$

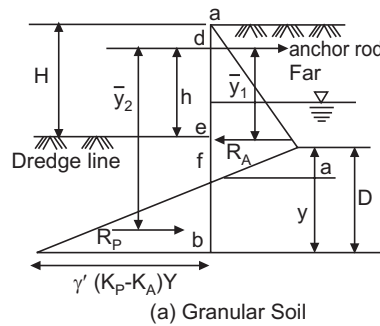
Anchored Bulkhead

If the wall height is large, support against lateral pressure is provided by embedment in the ground as well as by tie rods near the top. This type of earth retaining structure is called an anchored bulkhead.



(a) Anchored bulkhead in granular soil.

- F_{ar} = Force in anchor rod
- R_A = Resultant active earth pressure acting at \bar{y}_1 below the anchor rod level.
- R_p = Resultant passive earth pressure acting at \bar{y}_2 below the anchor rod.



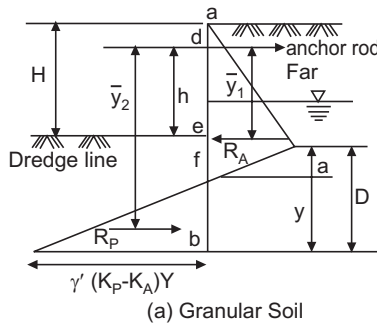
For equilibrium

$$F_{ar} + R_p - R_a = 0$$

Depth 'a' to the point of zero pressure

$$a = \frac{P_{AC}}{\gamma' (K_p - K_a)}$$

(b) Anchored bulkhead in cohesive soil.



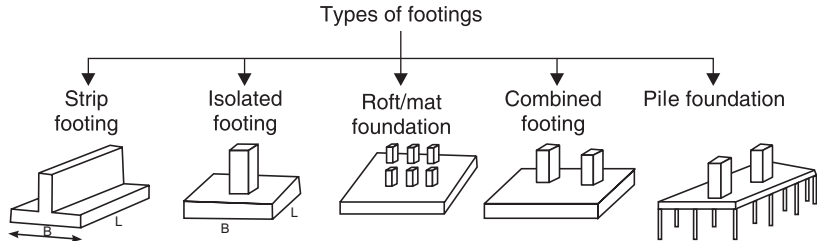
Coffer Dam: It is a temporary structure constructed usually in river lake etc to keep the working area dry for construction of other structure.

After the construction of coffer dam area is dewatered by pumping.

Types of coffer dam: Earth embankments, cantilever sheet pile, double wall coffer dam, braced coffer dans.

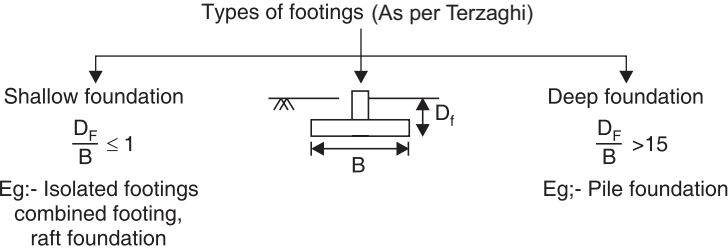
Shallow Foundation

Footings are the lower most supporting part of the structure known as sub-structure and are last structural elements through which load is transferred to foundation comprising soil/rock.



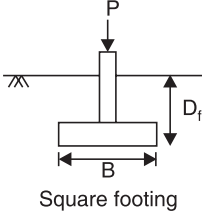
General requirement for foundation

- (a) Foundation must be safe against shear failure.
- (b) Settlement of the foundation should be within permissible limits.
- (c) Foundation should be located at such depth, such that its performance is not affected by seasonal volume changes.



Basic Definitions

- 1. Bearing Capacity:** The load carrying capacity of foundation soil or rock which enables it to bear and transmit loads from the structure.
- 2. Gross Pressure or Gross Loading Intensity (q_g):** It is the total pressure at the base of the footing due to weight of the super-structure,



self weight of the footing and weight of the earth fill.

$$q_g = \frac{P}{B^2} + \gamma D_f$$

- 3. Net Pressure Intensity:** Its the excess of gross pressure to over burden pressure.

$$q_{\text{net}} = q_g - \gamma D_f$$

For safe design

$$\frac{P}{B^2} \leq q_{\text{net-allowable}}$$

Note: If excavation is not backfilled (i.e. in case of basements)

$$q_{\text{net}} = \frac{P}{B^2} - \gamma D_f \quad \text{and} \quad \frac{P}{B^2} - \gamma D_f \leq q_{\text{net-allowable}}$$

In this case load carrying capacity of the soil is increased. If the raft is constructed at the depth such that $\frac{P}{B^2} - \gamma D_f = 0$, then soil is called

upon not to resist any load. Such as raft is called fully **compensated raft** or floating raft.

- 4. Ultimate bearing capacity (q_u):** The maximum grass intensity of loading that the soil can support before it fails in **shear** is called ultimate bearing capacity.
- 5. Net ultimate bearing capacity:** It is the minimum net pressure causing shear failure of soil.

$$q_{\text{nu}} = q_u - \gamma D_f = \frac{P}{B^2}$$

- 6. Net Safe bearing Capacity:**

$$q_{\text{ns}} = \frac{q_{\text{nu}}}{\text{FOS}}$$

where FOS of 2-3 is adopted.

- 7. Gross safe bearing Capacity:**

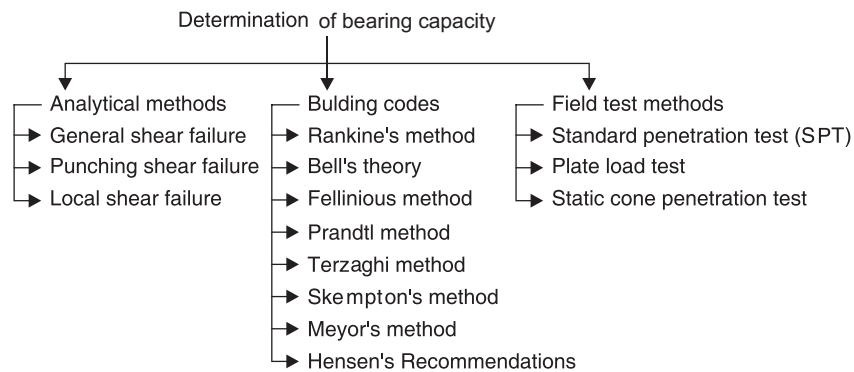
$$q_s = \frac{q_{\text{nu}}}{\text{FOS}} + \gamma D_f$$

- 8. Safe bearing Pressure:** Maximum net intensity of loading that can be allowed on soil without the **settlement** exceeding the permissible value.

Note: No factor of Safety is used when dealing with settlement.

9. Allowable bearing pressure: Maximum net intensity of loading that can be imposed on the soil with no possibility of **shear** failure or the possibility of **excessive** settlement.

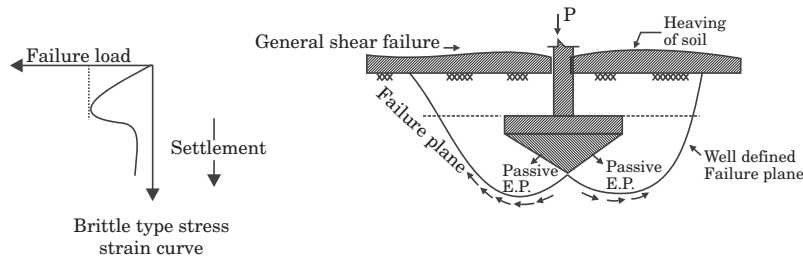
Note: It is smaller of Net safe bearing capacity and safe bearing pressure.



Analytical Method's

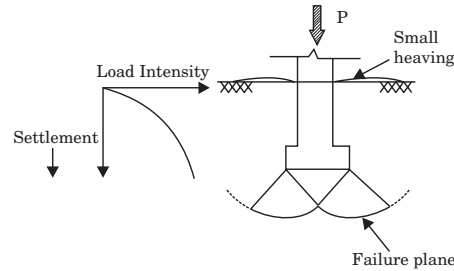
Based on shear failure criteria

1. General Shear Failure:



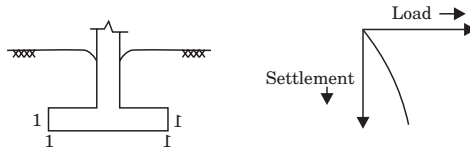
- Brittle type shear-stress curve
- Over consolidated clay with low compressibility
- Well defined failure pattern
- Failure due to tilting of foundation
- Occurs in soil with relative density $> 70\%$
- Occurs after plastic equilibrium state is reached.

2. Local Shear Failure:



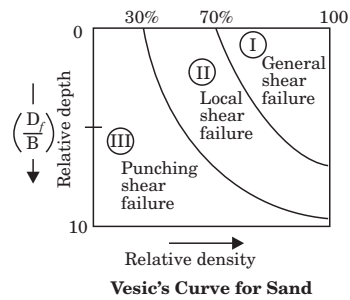
- Partial development of state of plastic equilibrium
- Slight heaving of soil adjacent to foundation
- Foundation doesn't tilt
- Failure is not sudden
- Plastic stress-strain curve
- Occurs in loose sand with relative density 30–70%

3. Punching Shear Failure:



- Shearing in vertical direction around the edge
- No heaving of adjacent soil
- No tilting of foundation
- Very loose sand with relative density less than 30%
- Deep foundations generally fail by punching only

Parameter	General shear failure	Local Shear failure
1. Friction angle(ϕ)	$> 36^\circ$	$< 28^\circ$
2. Strain at failure	$\leq 5^\circ$	$\geq 15^\circ$
3. SPT number	> 30	< 5
4. Relative density	$> 17\%$	$< 20\%$
5. Void ratio	< 0.55	> 0.75
6. Unconfined Compressive Strength	$> 100 \text{ KN/m}^2$	$< 80 \text{ KN/m}^2$

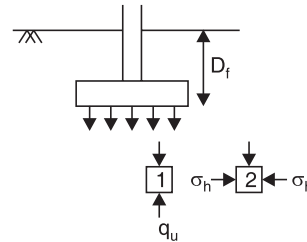


Building Codes

1. Rankine's Method (ϕ -soil):

$$q_u = \gamma D_f \tan^4 \left(45 + \frac{\phi}{2} \right)$$

$$q_u = \gamma D_f \left(\frac{1 + \sin \phi}{1 - \sin \phi} \right)^2$$

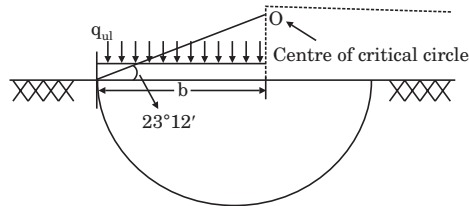


2. Bell Theory ($C - \phi$ soil):

$$q_u = CN_c + \gamma D_f N_q$$

for pure clays $C = 4, N_q = 1$

3. Fellenius Method (C -soil):



Location of critical circle for surface footing in Fellenius' method

Failure due to slip and consequent heaving of a mass of soil on one side

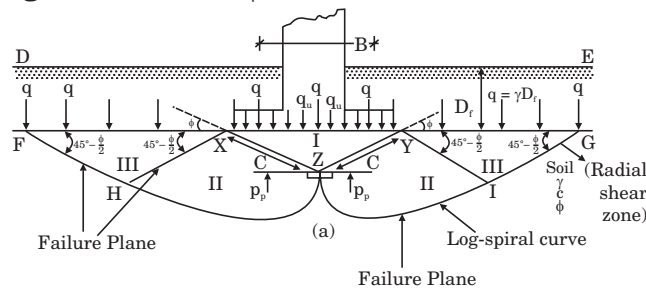
$$q_{ult} = \frac{Wlr + CR}{b \cdot lo} \qquad q_{ult} = 5.5 C$$

4. Prandtl Method ($C - \phi$ soil):

$$q_u = CN_c + rD_f N_q + 0.5 Br N_r \quad \text{for strip footing}$$

For C -soil $N_c = 5.14, N_q = 1, N_r = 0$

5. Terzaghi Method ($C - \phi$ soil):



- General shear failure governed by Mohr's criteria
- Strip footing at shallow depth ($D_f/B \leq 1$)
- Shear resistance of soil between ground surface and footing base is neglected

Zone I → Zone of elastic Equilibrium

Zone II → Radial Shear Zone

For C-soil → circular shape

C – ϕ soil → logarithmic shape

Zone III → Passive plastic Equilibrium with $\left(45 - \frac{\phi}{2}\right)$ angle with the Horizontal.

For strip footing,

$$q_u = CN_c + \gamma D_f N_q + 0.5 B \gamma N_r$$

$$q_{nu} = \underbrace{CN_c}_{\text{Cohesion}} + \underbrace{(\gamma D_f - 1)N_q}_{\text{Overburden}} + \underbrace{0.5 B \gamma N_r}_{\text{Soil in Shearing Zone}}$$

$$N_c = (N_q - 1) \cot \phi$$

$$N_q = \frac{a^2}{2 \cos^2 (45 + \phi/2)}$$

$$a = e^{(3\pi/4 - \phi/2) \tan \phi}$$

$$N_r = \frac{1}{2} \tan \phi \left[\frac{K_{p\gamma}}{\cos^2 \phi} - 1 \right]$$

Note: N_c , N_q , N_r are the function's of ϕ only. Even K_p (passive earth pressure coefficient) is also function of ϕ . Hence the bearing capacity increases as the value of ϕ increases.

$$\text{For clayey soil } (\phi = 0) \quad N_c = 5.7 \quad N_q = 1 \quad N_r = 0$$

Modification in Terzaghi's Equation

1. For Source footing

$$q_{nu} = 1.3 CN_c + q (N_q - 1) + 0.4 B \gamma N_r$$

2. For Circular footing

$$q_{nu} = 1.3 CN_c + q (N_q - 1) + 0.3 B \gamma N_r$$

3. For rectangular footing

$$q_{nu} = \left(1 + \frac{0.3 B}{L}\right) CN_c + q(N_q - 1) + \left(1 - \frac{0.2 B}{L}\right) (0.5 B \gamma N_r)$$

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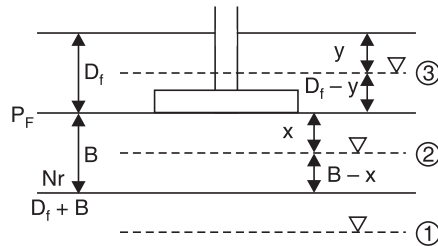
4. For local shear failure ($\phi < 29^\circ$)

$$C_m \rightarrow \frac{2}{3} C \quad (\tan \phi)_m = \frac{2}{3} \tan \phi$$

From C_m and ϕ_m find N_c', N_q', N_r'

$$q_{nu} = \frac{2}{3} CN_c' + q(N_q' - 1) + 0.5 B\gamma N_r'$$

5. For water table, in strip footing



(a) For (1) \rightarrow water table below $D_f + B$

$$q_{nu} = CN_c + \gamma_t D_f (N_q - 1) + 0.5 B \gamma_t N_r$$

(b) For (2) \rightarrow water table between D_f and $D_f + B$

$$q_{nu} = CN_c + \gamma_t D_f (N_q - 1) + 0.5 (x\gamma_t + (B - x)\gamma_{sub}) N_r D_f$$

(c) For (3) water table between 0 and D_f

$$q_{nu} = CN_c + [\gamma_t y + (D_f - y)\gamma_{sub}] (N_q - 1) + 0.5 B \gamma_{sub} N_r$$

Another way of modification due to water table

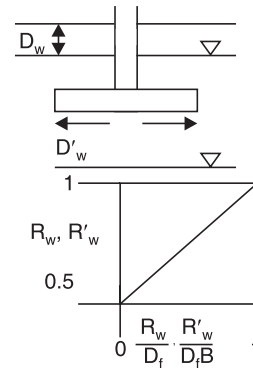
$$q_{nu} = CN_c + D_f r_t (N_q - 1) R_w + 0.5 B r_t N_r R_w'$$

$$R_w = 0.5 \left(1 + \frac{D_w}{D_f} \right)$$

when $0 < \frac{D_w}{B} \leq 1$

$$R_w' = 0.5 \left(1 + \frac{D_w'}{B} \right)$$

when $0 < \frac{D_w'}{B} < 1$



6. **Skempton's Method** (C-soil)

\Rightarrow Applicable only for saturated clay

\Rightarrow Applicable to deep foundations also.

$$q_{nu} = CN_C$$

'C' can be found out from

- (i) U-U test
- (ii) Uncombined compression test
- (iii) Vane shear test

For value of NC

(a) Strip footing

$$N_C = 5 \left(1 + 0.2 \frac{D_f}{B} \right), \frac{D_f}{B} < 2.5 \quad \text{for } \frac{D_f}{B} \geq 2.5 \quad N_C = 7.5$$

(b) Source/circular footing

$$N_C = 6 \left(1 + 0.2 \frac{D_f}{B} \right), \frac{D_f}{B} < 2.5 \quad \text{For } \frac{D_f}{B} \geq 2.5 \quad N_C = 9$$

(c) For rectangular footing

$$N_C = 5 \left(1 + 0.2 \frac{D_f}{B} \right) \left(1 + 0.2 \frac{B}{L} \right), \frac{D_f}{B} < 2.5$$

$$\text{For } \frac{D_f}{B} \geq 2.5 \quad N_C = 7.5 \left(1 + \frac{0.2 B}{L} \right)$$

7. Meyerhoff's Method (C-φ soil)

Applicable for both shallow as well as deep foundation.

Note: Failure surface is assumed to go above the foundation level.

$$q_u = CN_C S_C d_C i_C + qN_q S_q d_q i_q + 0.5 B \gamma N_\gamma S_\gamma d_\gamma i_\gamma$$

where S, d, i are empirical correlation factors for shape, depth, inclination. For φ-soil $N_C = 5.14$ $N_q = 1$ $N_\gamma = 0$

8. Hensen's Recommendations (φ-soil)

$$q_u = CN_C S_C d_C + qN_q S_q d_q i_q + 0.5 B \gamma N_\gamma S_\gamma d_\gamma i_\gamma$$

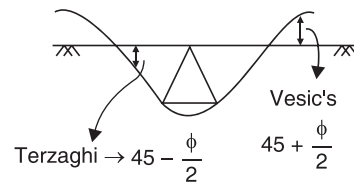
For φ = 0; $q_{nu} = CN_C (1 + S_C + d_C - i_C)$

9. Vesic's Bearing Capacity:

Failure surface assumed by Vesic is similar to Terzaghi but the angle of inclination of failure surface with the horizontal is

$45 + \frac{\phi}{2}$ rather than $45 - \frac{\phi}{2}$ as

given by Terzaghi.



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10. I.S. Code Method (IS 6403–1981):

$$q_{nu} = CN_C (S_C d_C i_C) + q(N_q - 1) (S_q d_q i_q) + 0.5B\gamma N_\gamma (S_\gamma d_\gamma i_\gamma) W'$$

$N_C, N_q, N_\gamma \rightarrow$ From Vedic's equation

$W' \rightarrow$ water table correction factor

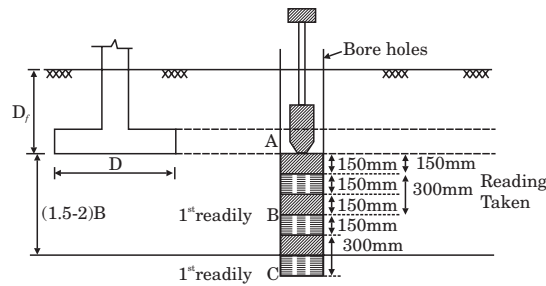
$\Rightarrow W' = 1$ if water table below $D_f + B$

$\Rightarrow W' = 0.5$ if water table at D_f

\Rightarrow Interpolation if water table between D_f and $D_f + B$

Field Tests

1. Standard Penetration Test



\Rightarrow For Granular soils only

\Rightarrow N-value is determined at selected number of bore holes and avg. value of corrected N is calculated for the depth from $D_f + (1.5 - 2)B$.

\Rightarrow Any value greater than 50% of the avg. value is discarded and new avg. value is found out.

\Rightarrow

N	ϕ	Relative Density
< 4	25-30	0
4-10	27-32	15

\Rightarrow Over burden Correction

$$N_1 = N_0 \left(\frac{350}{\bar{\sigma} + 70} \right)$$

$N_0 =$ observed SPT value

$N_1 =$ Corrected N value of overburden

$$\bar{\sigma} \leq 280 \text{ KN/m}^2 \text{ So } N_1 > N_0$$

\Rightarrow Dilatancy correction required only in saturated fine sand or silt

\Rightarrow More significant in case of fine dense sand ($N_1 > 15$) as it has tendency to dilate under rapid loading and -ve pore pressure will develop.

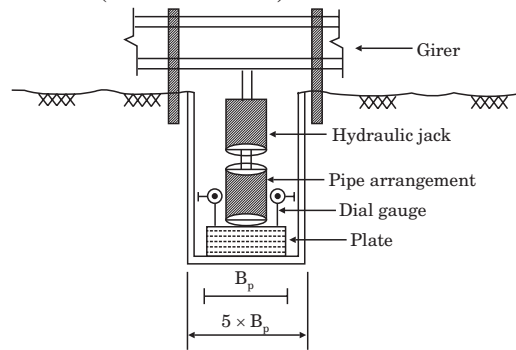
$$N_2 = 15 + \frac{1}{2}(N_1 - 15)$$

⇒ **Teng's Formula** for q_{nu} in granular soil.

$$q_{nu} = \frac{1}{6} (3N^2 BR_w' + 5(100 + N^2) D_f R_w). \text{ Continuous or strip footing}$$

$$q_{nu} = \frac{1}{3} (N^2 BR_w' + 3(100 + N^2) D_f R_w) \text{ Square or circular footing}$$

2. Plate load test: (IS 1888-1992)



It is used to calculate

- (a) Ultimate bearing capacity
- (b) Allowable bearing capacity
- (c) Safe settlement of foundation

⇒ Significant only for cohesionless soil

For Clayey soil

$$\frac{q_{uf}}{S_f} = \frac{q_{up}}{S_p} = \frac{B_f}{B_p}$$

For Granular Soil

$$\frac{q_{uf}}{q_{up}} = \frac{B_f}{B_p}$$

$$\frac{S_f}{S_p} = \left[\frac{B_f}{B_p} \left(\frac{B_p + 0.3}{B_f + 0.3} \right) \right]^2 \quad B_f, B_p \text{ in metres}$$

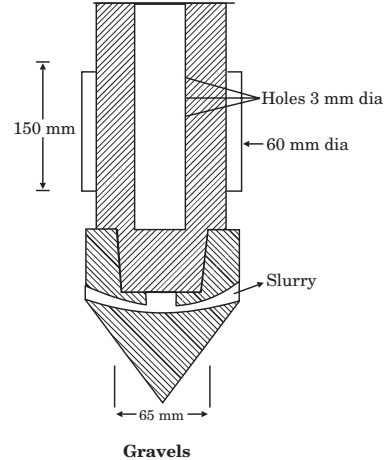
Depth Correction

$$S_f(\text{correction}) = S_f \left(\frac{1}{1 + \frac{D_2}{B_f}} \right)^{0.5}$$

D_2 = depth of foundation from the level at which plate load test is carried out.

3. State cone penetration test (CPT):

- ⇒ Particularly for soft clays, silts and fine to medium sand deposits.
- ⇒ Continuous record of soil resistance
- ⇒ Cone area 10 cm², Apex angle 60°
- ⇒ Rate of pushing cone 20 mm/sec upto depth of 100 mm.



Allowable Bearing Capacity ($Q_{A,net}$)

It is the **minimum** of bearing strengths obtained from shear failure criteria and settlement criteria. Empirical relations for Q_A are:

1. Peak Henson's Formula

$$q_{a(net)} = 0.44 NS C_w$$

$$C_w = 0.5 \left(1 + \frac{D_w}{D_f + B} \right)$$

- N = corrected SPT N-value
- S = Permissible settlement (mm)
- C_w = Water table correction factor
- D_w = depth of WT below ground

2. Teng's formula:

$$q_{a(net)} = 1.4(N-3) \left(\frac{B + 0.3}{2B} \right)^2 \cdot S \cdot C_w \cdot C_D$$

C_D = depth correction factor

$$C_w = 0.5 \left(1 + \frac{D_w}{B} \right)$$

$$C_D = \left(1 + \frac{D_f}{B} \right) \leq 2$$

3. I.S. Method for Raft:

$$q_{net}(safe) = 0.88 N S C_w$$

C_w → from Peek henson's

Settlement of foundation:

$$S = S_{\text{immediate}} + S_{1^{\circ}} + S_{2^{\circ}}$$

$$\text{Where } S_{\text{immediate}} = \frac{q_n B(1 - \mu^2)}{E_s} \times I_f$$

$S_{\text{immediate}} \Rightarrow$ Elastic settlement for both sandy and clayey soil
 $\mu =$ Poisson's ratio

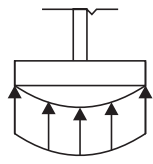
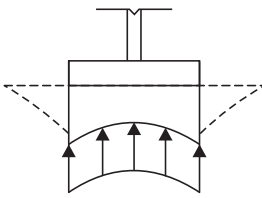
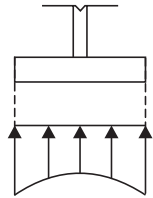
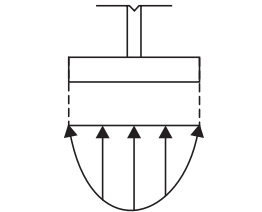
$E_s =$ modular of elasticity

$I_f =$ Influence factor = $f(\text{shape, rigidity of structure})$

E_s can be calculated from Triaxial tests or field tests.

$$S_{\text{rigid immediate}} = S_{\text{flexible immediate}} \times 0.8$$

Deflected Shape of Footings

	Clayey Soil	Granular soil
Flexible Footing Settlement varies Pressure constant		
Rigid Footing Settlement constant Pressure varies		

Permissible Settlements in Shallow Foundation

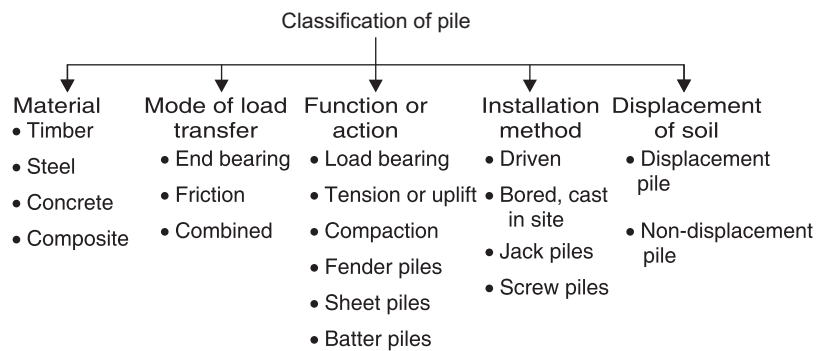
	Total settlement (mm)	Differential Settlement (mm)	Angular distortion (mm)
Isolated footing on clay	65	0.0015L	1/666
Isolated footing on sand	40	0.0015L	1/666
Raft on clay	65-100	0.0021L	1/500
Raft on sand	40-65	0.0021L	1/500

Deep Foundation

When the soil at shallow depth is poor and the load to be transmitted is heavy then the depth of the foundation has to be increased till the suitable soil strata is met, such foundation are called deep foundations.

Pile: Small dia shaft which is driven or bored into ground.

Piers and wells: large diameter shafts constructed by excavation and sunk to required depth.



End bearing piles: Used in stiff clay. Dense sand.

Friction pile: Used in soft soil, clay.

Tension or uplift piles: anchor structures subjected to **hydrostatic pressure or overturning moment**.

Compaction pile: compact loose granular soil

Anchor pile: Anchor against **horizontal pull** from water or sheet piling.

Fender pile: protect water-front structures against **impact from ships** and other floating objects.

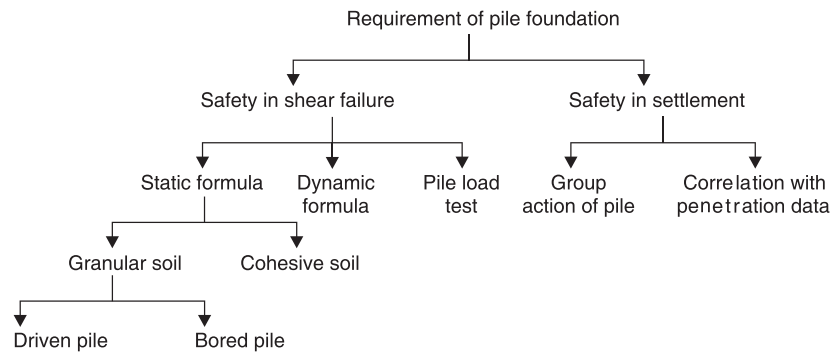
Sheet piles: Used as cut-offs to reduce seepage and uplift in hydraulic structure.

Batter piles: Resist horizontal and inclined forces, especially in water front structure.

Displacement piles: It displaces the pile laterally or upward. In loose sand, a pile densifies the sand upto a distance of 3.5 times the diameter of pile measured from the centre of pile. In case of clays, large displacement piles remould the soil to a distance of 2 times the diameter of pile.

Non-displacement piles: Are bored piles. Such piles are formed in the soil by boring or excavation and then these voids are filled with concrete sides are either supported by casing or by Bentonite slurry.

Note: Driven concrete piles are generally of diameter upto 500 mm. But bored piles may be even 2-3 m.



1. Static formula

$$Q_u = Q_{pu} + Q_f$$

Q_u = Ultimate load

Q_{pu} = Ultimate point load

Q_f = Ultimate skin friction.

$$Q_{pu} = q_{pu} \cdot A_b$$

$$Q_f = F_s \cdot A_s$$

q_{pu} = Unit point bearing resistance

A_b = Area of base

F_s = Unit skin friction resistance

A_s = Surface area of pile in contact with soil.

So $Q_u = q_{pu} A_b + F_s A_s$

For C - ϕ soil $q_{pu} = CN_c + \gamma D_f N_q + 0.5 B \gamma N_\gamma$

Neglect $0.5 B \gamma N_\gamma$ wrt. γD_f as $B \ll D_f$

Hence, $q_{pu} = CN_c + \gamma D_f N_q$

for C - soil $q_{pu} = CN_c$

for ϕ - soil $q_{pu} = \gamma D_f N_q$

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(a) static formula in driven granular soil.

$$Q_u = (\gamma D_f N_q) A_b + F_s A_s$$

where $F_s = K \sigma_{avg} \tan \delta$

For loose sand to from loose to medium sand $D_f = 15$ (dia of pile)

For dense sand $D_f = 20$ (dia of pile)

For values of K and S

Pile material	δ	Value of K	
		Loose	Dense
Steel	20°	0.5	1
Concrete	3/4 ϕ	1	2
Timber	2/3 ϕ	1.5	4.0

Note: As per IS code $\delta = \phi$ and $K = 1 - 3$ for driven piles in loose to medium sand

When there are several layers of soil then

$$Q_p = K \tan \delta (\sigma_{avg1} \cdot A_1 + \sigma_{avg2} A_2 + \dots + \sigma_{avgn} A_n)$$

(b) Static formula in bored granular soil.

Point bearing of bored cast in situ piles = $\frac{1}{2} \times$ point bearing resistance of driven piles.

Due to boring, the value of K becomes very small and taken as 0.5. Rest all calculations as above.

Note: Maximum upper limit of frictional stress (f_s) is = 110 KN/m²
Maximum upper limit of point bearing stress.

(a) 11000 KN/m² → silica sand

(b) 5000 KN/m² → calcareous sand

(c) Static formula for piles in clay.

$$Q_u = (C_{ub} N_c) A_b + (\alpha C_u) A_s$$

C_{ub} = Undrained cohesion at the base of the pile

C_u = Undrained cohesion in the embedded length of pile.

$N_c = 9$ (By **skempton's**).

α = Depends on adhesion between soil and pile called adhesion factor

$\alpha = 0.1$ → for very loose clays

$\alpha = 0.3$ → for very stiff clays

Note: Smaller the undrained strength, softer is the consistency and greater is the tendency to adhere to the pile.

2. Dynamic formula: It is based on resistance to penetration hence used in driven piles only

Energy Imparted = Work done in pile driving

$$Q_u \times S = W \times H$$

(a) Engineering News Formula

$$Q_{\text{allowable}} = \frac{WH}{\text{FOS}(S + C)}$$

W = load in Kg

H = Height of fall in cm

S = Settlement/blow in cm

= It is corresponding to last 5-blows of drop hammer also called, as real set per blow.

= last 20 blows of steam hammer.

C = Emperical factor

= 2.5 cm for drop hammer

= 0.25 cm for single acting steam hammer.

FOS = 6

Another form: $Q_{\text{KN}} = \frac{166.64 E_{\text{KJ}}}{S + 2.54}$

S = Settlement/Avg penetration for last 100 mm of driving per blow. Minimum permissible value of S = 1.25 mm.

(b) Modified Hilly Formula:

$$\text{Ultimate Driving Resistance (R)} = \frac{Wh\eta}{S + \frac{C}{2}}$$

W = Weight of hammer (Tonnes)

h = Ht of fall (cm)

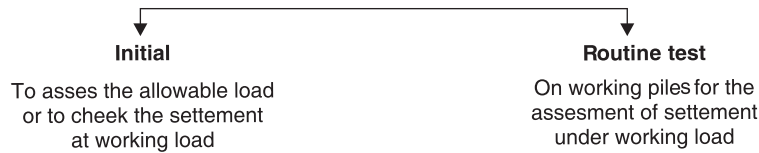
S = Final set per blow (last- one - cm)

C = Total elastic compression per blow ie of soil

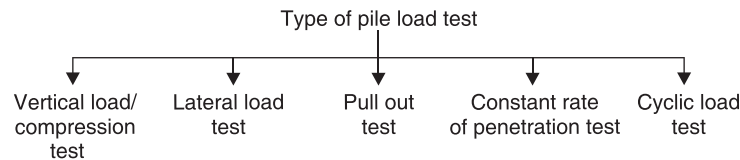
+ pile + Dolly

η = Efficiency of blow.

3. Pile load test: (IS 2911) It is the only direct method for determining the allowable loads on the piles and, is considered to be most reliable as it is an insitu test.



Note: As per IS code, for more than 200 piles there should be a minimum of two initial test where as routine test is done on 0.5% to 2% of total number of piles.

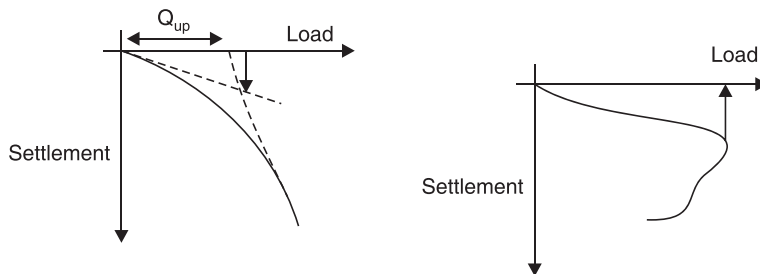


Cyclic load: test is carried out to determine **skin friction and end bearing separately** for a pile load on a single pile. It is generally an initial test.

Note: Test pile is a pile which is especially bored for the purpose of conducting test and will not be the part of foundation in future.

While working pile is a pile which is a part of foundation and is being used for the purpose of testing at present.

Ultimate load will be calculated from the load settlement curve



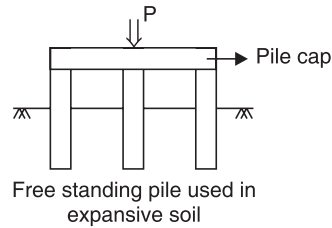
Allowable load on single pile: Will be the minimum of the following cases.

- (i) 50% of the ultimate load at which total settlement is equal to the 1/10 of the pile diameter.
- (ii) 2/3rd of the load at which total settlement is 12 mm.
- (iii) 2/3rd of the load at which net settlement is 6 mm (total settlement – elastic settlement)

Group Action of Piles

When piles are driven there is uncertainty regarding vertical installation of piles.

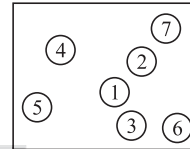
Hence minimum number of piles driven are 3. where in case of bored piles single pile can also be used.



Note: To void tightening of ground, pile in sand should begin at centre and then moved out-ward. (numbering in while piles to be driven)

$$\text{Group efficiency } \eta = \frac{Q_{ug}}{n Q_u}$$

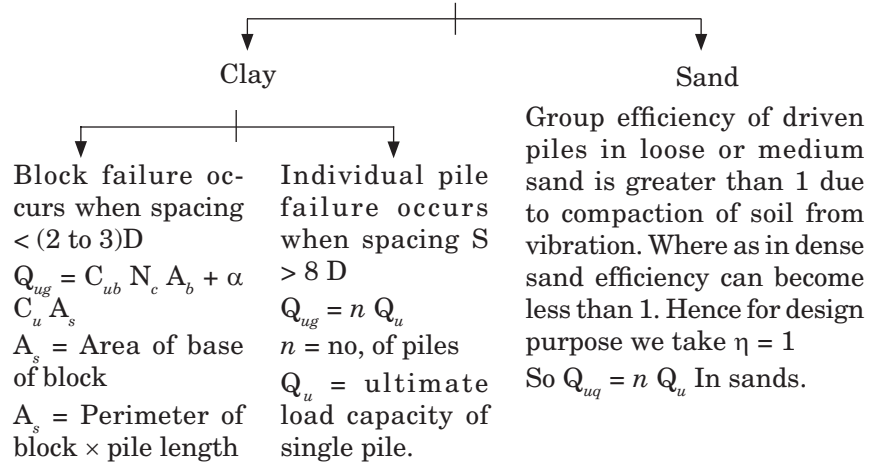
- Q_{ug} = ultimate load capacity of pile group
- Q_u = ultimate load capacity of single pile
- n = No. of piles.



Note: Minimum spacing between piles according to I.S code
 For loose sand or back filled soil = $2 \times \text{Diameter}$
 For point bearing piles = $2.5 \times \text{Diameter}$
 For friction piles = $3 \times \text{Diameter}$.

In case of non-circular piles, diameter of the circumscribed circle is taken as diameter

Ultimate bearing capacity of pile group.



Safe load capacity

$$Q_s = \left[\frac{\text{minimum of } [Q_{ug}, n Q_u]}{\text{F.O.S}} \right]$$

Converse labarre pile group efficiency

$$\eta_g = 1 - \frac{\theta}{90} \left[\frac{(n-1)m + (m-1)n}{mn} \right]$$

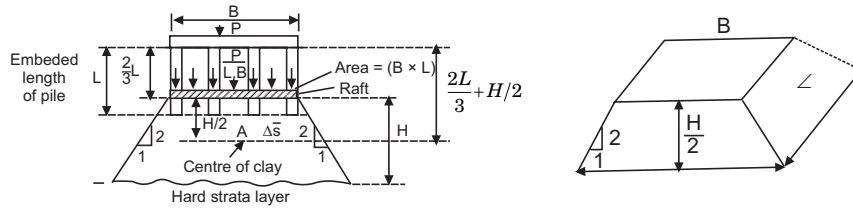
$$\tan \theta = \frac{d}{s}$$

- $d = \text{diameter of pile}$
- $s = \text{centre to centre spacing.}$
- $m = \text{no. of rows}$
- $n = \text{no. of piles in a row.}$

Settlement of pile groups

As the zone of influence of pile group is generally more than the individual pile so settlement of pile group is generally greater than the settlement of individual pile to same loading. (ie same load per pile)

1. Settlement of pile group in clays

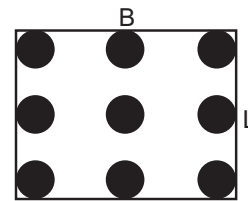


(a) When pile is in uniform clay deposit

$$\Delta H = \frac{C_C}{1 + e_o} H \log \left(\frac{\bar{\sigma}_o + \Delta \bar{\sigma}}{\bar{\sigma}_o} \right)$$

$$\bar{\sigma}_o = \left(\frac{2}{3} L + \frac{H}{2} \right) \gamma_t$$

$$\Delta \bar{\sigma}_o = \frac{P}{\left(B + \frac{H}{2} \right) \left(L + \frac{H}{2} \right)}$$



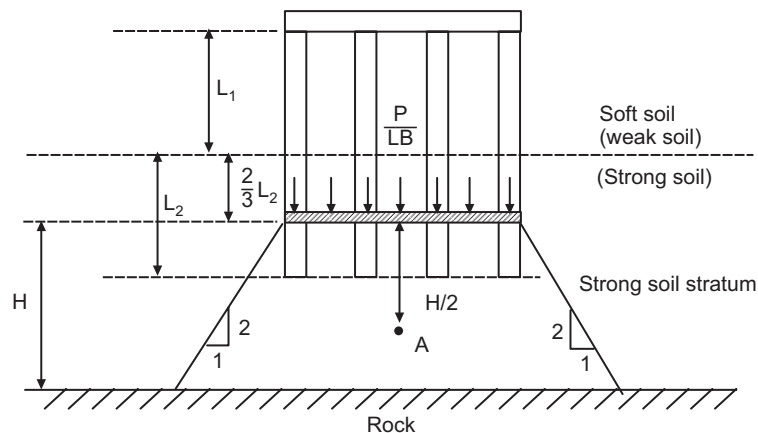
(b) When piles are driven into strong stratum through an overlaying weak stratum

Here depth H is measured from $\frac{2}{3} L_2$ to the bottom solid surface

where L_2 is the depth of embedment in strong soil.

$$\Delta H = \frac{C_C}{1 + e_o} H \log \left(\frac{\bar{\sigma}_o + \Delta \bar{\sigma}}{\bar{\sigma}_o} \right)$$

where $\bar{\sigma}_o$ is measured at point A (mid depth of H)

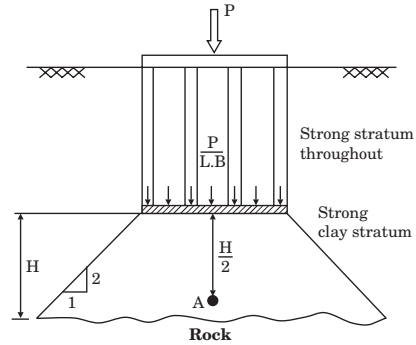


(c) In case of bored piles or end bearing piles resting on firm stratum

Here H is measured from the bottom of piles to the bottom hard strata

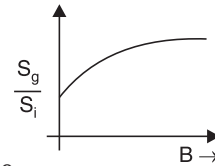
$$\Delta H = \frac{C_C}{1 + e_o} H \log \left(\frac{\bar{\sigma}_o + \Delta \bar{\sigma}}{\bar{\sigma}_o} \right)$$

$\bar{\sigma}_o$ = effective stress at point A



2. Settlement of pile groups in sand

$$\text{Group settlement ratio} = \frac{S_g}{S_i} = \left(\frac{4B + 2.7}{B + 3.6} \right)^2$$



S_g = Group settlement at the same load of pile group.

B = Size of pile group in meter.

S_i = Settlement of individual pile calculated from the pile load test